

# **Theory of the Firm**

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## **Boundaries of the Firm**

- Firms are economic units that make decisions, produce, sell, etc.
- What determines the optimal size of a firm? Should two plants be organized as two independent firms or as two divisions in one firm?
- Traditional economic analysis is silent about these issues, and takes the size of the firm as given.
- Moral hazard theory, with the exception of its multitasking part, also takes the size of the firm as given.

# Grossman and Hart (1986): Incomplete Contracts and Property Rights

- Some states of the world cannot be contracted upon:
  - Agents cannot think about all contingencies.
  - They cannot communicate and negotiate about all possibilities.
  - They cannot write a clear contract that courts can then enforce.
- If contracts cannot fully specify the usage of the asset in every state of the world, then who gets the right to choose?

- The owner can decide on the usage, when unspecified by contract.
  - Contracts provide specific property rights, while ownership provides **residual property rights**.
- The owner of an asset will have a stronger incentive to make asset-specific investments, knowing that he has residual property rights.
- Transferring ownership of an asset from one party to another has a benefit – encouraging investment by the acquirer – and a cost – discouraging investment by the acquired. The tradeoff generates implications for ownership structures and firm boundaries.

## A Basic Model (Hart, Ch. 2)

- There are two assets,  $a1$  and  $a2$ , and two managers,  $M1$  and  $M2$ .
- $a2$  in combination with  $M2$  can supply a unit of input to  $M1$ , who, in combination with  $a1$ , can use it to produce a unit of output and sell it on the market.
- There are two dates, 0 and 1:
  - At date 0,  $M1$  and  $M2$  make (human-capital) investments to improve productivity. Those are denoted as  $i$  and  $e$ , respectively.

- At date 1,  $M1$  and  $M2$  decide whether to conduct the transaction between them or go to the market.
- At date 0, it is too costly to write a contract on the date-1 use of the assets. The owner of an asset will have the right to choose.
- Three ownership structures are considered:
  - Non-integration:  $M1$  owns  $a1$  and  $M2$  owns  $a2$ .
  - Type-1 integration:  $M1$  owns  $a1$  and  $a2$ .
  - Type-2 integration:  $M2$  owns  $a1$  and  $a2$ .

## Date-1 Payoffs and Surplus

- At date 1,  $M1$  receives:
  - If trade occurs between  $M1$  and  $M2$ ,  $M1$  receives  $R(i) - p$ .
  - If trade does not occur,  $M1$  buys the input in the market and receives:  $r(i, A) - \bar{p}$ .
    - The revenue is different for the lack of  $M2$ 's human capital.
    - $A$  denotes the assets that  $M1$  owns, and can be  $\{a1\}$ ,  $\{a1, a2\}$ , or  $\emptyset$ .

- Similarly, for  $M2$ :
  - If trade occurs between  $M1$  and  $M2$ ,  $M2$  receives  $p - C(e)$ .
  - If trade does not occur,  $M2$  sells the input in the market and receives:  $\bar{p} - c(e, B)$ .
    - $B$  denotes the assets that  $M2$  owns:  $\{a2\}$ ,  $\{a1, a2\}$ , or  $\emptyset$ .
- The surplus in case of trade is  $R(i) - C(e)$ , while in case of no trade it is  $r(i, A) - c(e, B)$ .
- Assuming gains from trade: For all  $i$  and  $e$  and  $A$  and  $B$ :

$$R(i) - C(e) \geq r(i, A) - c(e, B).$$



## Date-1 Division of Surplus

- Ex-post, at date-1, for a given ownership structure and investments, the parties can negotiate. Hence, they choose to trade.
- It is assumed that the gains from trade  $[(R - C) - (r - c)]$  are divided half-half, as in the **Nash bargaining solution**.
- The profits of  $M1$  and  $M2$  are then:

$$\begin{aligned}\pi_1 &= R - p = r - \bar{p} + \frac{1}{2} [(R - C) - (r - c)] \\ &= -\bar{p} + \frac{1}{2} (r + R - C + c),\end{aligned}$$

$$\begin{aligned}\pi_2 &= p - C = \bar{p} - c + \frac{1}{2} [(R - C) - (r - c)] \\ &= \bar{p} - \frac{1}{2} (r - R + C + c).\end{aligned}$$

- The price is given by:  $p = \bar{p} + \frac{1}{2} [(R - r) - (c - C)]$ .
  - Note that integration involves transformation of ownership of physical capital, but not of human capital (e.g., under type-1 integration,  $M1$  controls  $a2$ , but has no say on what  $M1$  does).
  - The division of surplus is independent of ownership structure.

## Return on Investment

- Key assumption is that marginal return on investment is increasing in how many assets in the relationship the investor has access to.
- For  $M1$ :

$$R'(i) > r'(i, \{a1, a2\}) \geq r'(i, \{a1\}) \geq r'(i, \emptyset),$$

○ where  $R', r' > 0; R'', r'' < 0$ .

- Similarly, for  $M2$ :

$$|C'(e)| > |c'(e, \{a1, a2\})| \geq |c'(e, \{a2\})| \geq |c'(e, \emptyset)|,$$

○ where  $C', c' < 0; C'', c'' > 0$ .

## First-Best Investment

- If the two parties could coordinate their investment decisions, they would reach a solution that maximizes the total surplus:

$$R(i) - i - C(e) - e.$$

- Denoting the first-best solution by  $(i^*, e^*)$ , we get:

$$R'(i^*) = 1,$$

$$|C'(e^*)| = 1.$$

- Yet, the parties are not able to coordinate or write a contract on their investment levels. These are **observable but not verifiable**.

## Investment Choice

- $M1$  and  $M2$  choose their investments non-cooperatively, each one maximizing his expected utility, taking the other's investment as given (Nash Equilibrium).
- $M1$  chooses  $i$  to maximize:

$$\pi_1 - i = -\bar{p} + \frac{1}{2} (r(i, A) + R(i) - C(e) + c(e, B)) - i,$$

○ leading to the following first-order condition:

$$\frac{1}{2} (r'(i, A) + R'(i)) = 1.$$

- $M2$  chooses  $e$  to maximize:

$$\pi_2 - e = \bar{p} - \frac{1}{2} (r(i, A) - R(i) + C(e) + c(e, B)) - e,$$

- leading to the following first-order condition:

$$\frac{1}{2} (|c'(e, B)| + |C'(e)|) = 1.$$

- We can immediately see that the equilibrium levels of  $i$  and  $e$  are below the first-best:

- $r'(i, A) < R'(i)$  and  $|c'(e, B)| < |C'(e)|$ .

## Why We Don't Achieve First-Best?

- The parties do not internalize the full benefit of the investment.
  - When  $MI$  invests, the return increases by  $R'$ .
  - However,  $MI$  realizes only:
    - $r'$ : direct benefit.
    - $\frac{1}{2}(R' - r')$ : share in surplus.
  - The sum of  $r'$  and  $\frac{1}{2}(R' - r')$  is lower than  $R'$ . This is a reflection of a **hold-up** problem.

## The Effect of Ownership

- The ownership structure determines the return a party gets on its investment in the case of no trade.
- Using subscripts 0, 1, and 2, to denote no integration, type-1 integration, and type-2 integration, respectively, we get that:

$$i^* > i_1 \geq i_0 \geq i_2,$$
$$e^* > e_2 \geq e_0 \geq e_1,$$

- Giving ownership to one party increases its investment and reduces the other party's investment.



## Optimal Ownership

- Optimal ownership maximizes the total surplus.
- We choose between:

$$S_0 = R(i_0) - i_0 - C(e_0) - e_0,$$

$$S_1 = R(i_1) - i_1 - C(e_1) - e_1$$

$$S_2 = R(i_2) - i_2 - C(e_2) - e_2.$$

- We can easily imagine establishing optimal ownership if one party is unique and is offering the reservation utility to the other party.

## Implications

- Overall, optimal ownership finds the balance between the effect on  $M1$ 's investment and the effect on  $M2$ 's investment.
  - In general, transferring ownership from one party to another increases one type of investment and decreases the other.
- If  $M1$ 's ( $M2$ 's) investment is inelastic, such that he chooses the same investment under all ownership structures, then type-2 (type-1) integration is optimal.

- No point of giving ownership to someone who doesn't respond to incentives.
- If  $M1$ 's ( $M2$ 's) investment is relatively unproductive, then type-2 (type-1) integration is optimal.
  - Investment being relatively unproductive can be captured by surplus decreasing to  $\theta(R(i) - i)$ , and  $\theta$  being sufficiently small.
  - No point of giving ownership to someone whose investment is not important.

- If assets  $a1$  and  $a2$  are independent,  $r'(i, \{a1, a2\}) = r'(i, \{a1\})$  and  $c'(e, \{a1, a2\}) = c'(e, \{a2\})$ , then non-integration is optimal.
  - There is no benefit, only cost, from shifting ownership on  $a1$  from  $M1$  to  $M2$ .
- If assets  $a1$  and  $a2$  are strictly complementary,  $r'(i, \{a1\}) = r'(i, \{\emptyset\})$  or  $c'(e, \{a2\}) = c'(e, \{\emptyset\})$ , then some form of integration is optimal.
  - Once a party does not control one asset, there is no additional cost, only benefit, from taking the other asset out of his control.

- Complementary assets should be owned by the same party (but not under joint ownership).
- If one party's human capital is essential, e.g., for  $M1$ ,  $c'(e, \{a1, a2\}) = c'(e, \{\emptyset\})$ , he should own both assets.
  - No point in giving ownership to a party when the other party is essential for the relationship.
- If both human capitals are essential, all ownership structures are equally good.
  - In this case, no party benefits from ownership without trade.

## **Hart and Moore (1990): Extending the Property-Rights Theory**

- The Grossman-Hart model reviewed above may seem a bit special as it only talks about the incentives of managers/entrepreneurs.
- Hart and Moore (1990) consider broader implications by asking what ownership does to employees' incentives.
- The identity of the owner of the assets will affect the incentives of employees, who are linked to the assets.

## Basic Setup

- The economy consists of a set  $\underline{S}$  of  $I$  risk neutral individuals, and a set  $\underline{A}$  of  $N$  assets  $(a_1, \dots, a_N)$ .
- There are two dates. At date 0, agent  $i$  makes a human-capital investment  $x_i$  ( $x = (x_1, \dots, x_I)$ ) At date 1, agents produce and trade.
- The cost of investment is  $C_i(x_i)$ , where  $C_i'(x_i) > 0$  and  $C_i''(x_i) > 0$ .
- Agents decide on investments non-cooperatively, and then, given investments, gains from trade are determined via bargaining.

## Date-1 Coalitions and Surplus

- At date 1, agents can form coalitions to use the assets in their control.
- Coalition  $S$  of agents, controlling subset  $A$  of assets, generates value of  $v(S, A|x)$ .
  - Assets controlled by coalition  $S$  denoted as  $\alpha(S)$ .
  - Control means either that an agent in the coalition owns the assets or that agents in the coalition together have majority.



- Value is increasing in assets and agents in the coalition, so optimal value ex-post for a given  $x$  is  $v(\underline{S}, \underline{A}|x) \equiv V(x)$ .
- Agents achieve this via negotiation.
- They split the value among them according to **Shapley values**:

$$B_i(\alpha|x) = \sum_{S|i \in S} p(S)[v(S, \alpha(S)|x) - v(S \setminus \{i\}, \alpha(S \setminus \{i\})|x)]$$

- The logic is to compensate the agent for his marginal contribution to a coalition, and calculate an average across all coalitions.

○ Here,  $p(S) = \frac{(s-1)!(I-s)!}{I!}$  is the probability of ending up in coalition  $S$  with random ordering.

- $s$  is the number of agents in coalition  $S$ .

○  $v(S, \alpha(S)|x)$  is the value achieved by the coalition when agent  $i$  is included, and  $v(S \setminus \{i\}, \alpha(S \setminus \{i\})|x)$  is the value achieved when the agent is excluded.

- From every coalition, the agent gets the difference between the two, which summarizes his marginal contribution.

## Date-0 Investment

- In Coalition  $S$ , agent  $i$ 's marginal return on investment is:

$$\frac{\partial v(S,A|x)}{\partial x_i} = v^i(S,A|x)$$

- $v^i(S, A|x) \geq 0$  and  $v^{ii}(S, A|x) \leq 0$ .

- $v^i(S, A|x) = 0$  if  $i \notin S$ .

- $\frac{\partial v^i(S,A|x)}{\partial x_j} \geq 0$  for all  $j \neq i$ .

- $v^i(S, A|x) \geq v^i(S', A'|x)$  for all  $S' \subseteq S$  and  $A' \subseteq A$ .

## Social Optimum

- The first-best solution maximizes surplus assuming that the grand coalition  $\underline{S}$  will form:

$$\max_x W(x) \equiv V(x) - \sum_{i=1}^I C_i(x_i)$$

- Hence, the first order condition for all  $i$  characterizing the first best  $x^*$  is:

$$v^i(\underline{S}, \underline{A} | x^*) = C'_i(x_i).$$

## Investment in a Non-Cooperative Equilibrium

- Agent  $i$  chooses investment to maximize the difference between his return (based on Shapley value) and cost. This yields the following first-order condition given the equilibrium behavior of others  $x^e(\alpha)$ :

$$\frac{\partial B_i(\alpha|x)}{\partial x_i} = \sum_{S|i \in S} p(S) v^i(S, \alpha(S) | x^e(\alpha)) = C'_i(x_i^e(\alpha))$$

- The right-hand side is clearly below  $v^i(\underline{S}, \underline{A} | x)$  for a given  $x$ , and this reflects under-investment.

- Based on this observation, Hart and Moore show that the equilibrium vector of efforts will exhibit under-investment.
- The intuition is similar to that in Grossman and Hart (1986):
  - When deciding on his level of investment, an individual doesn't consider the full benefit, but rather only what additional benefit the investment will give him in the bargaining process.
  - Hence he ignores the externality and ends up under-investing.
- Ownership affects what agents internalize and how much they invest.

## Optimal Ownership: Some Results

- When only one agent makes investment, he should own all assets.
  - As in Grossman and Hart (1986), shifting ownership from one agent to another decreases the investment of the first and increases the investment of the other.
    - An agent's incentive to invest is affected by the assets controlled by coalitions he is part of.
  - When only one agent is investing there is no tradeoff.

- For any coalition of agents, an asset should be owned by the coalition or its complement.
  - Since incentive to invest comes from assets owned by a coalition, there is waste in leaving an asset ‘not owned’.
  - A direct implication is that not more than one agent should have veto power over an asset.
    - Otherwise, if two agents are not in the same coalition and they share control, the asset is not owned by the coalition or its complement.



- If an agent is *indispensable* to an asset, then he should own it.
  - The definition is that without agent  $i$  in the coalition, the asset has no effect on the marginal product of investment for the other members of the coalition:

$$v^j(S, A) = v^j(S, A \setminus \{a_n\}) \text{ if } i \notin S.$$

- The asset encourages investment only when it is owned by a coalition that has agent  $i$ . To maximize such coalitions, we let the agent own the asset.
- This shows the effect of ownership on the investments of others.

- If an agent is *dispensable* and makes no investment, he should not have any control rights.

- The definition is that other agents' marginal product from investment is unaffected by whether the agent is in the coalition or not:

$$v^j(S, A) = v^j(S \setminus \{k\}, A) \text{ if } j \in S, j \neq k$$

- Reducing the agent's ownership will not reduce others' investments by the above definition.
- The agent himself is not investing.

- *Complementary* assets should always be controlled together.
  - Definition is that the two assets are unproductive unless they are used together:
 
$$v^i(S, A \setminus \{a_m\}) = v^i(S, A \setminus \{a_n\}) = v^i(S, A \setminus \{a_m, a_n\}) \text{ if } i \in S.$$
  - The idea is that by grouping the two assets in the same ownership, we make sure that in all coalitions with one asset, the other one will be as well.
  - Otherwise, there is waste, since each asset makes a contribution only with the other one on board.

## Clarifying the Role of Employees: Example

- Suppose that there are two assets  $a_1$  and  $a_2$ .
- Each asset has a big worker (potentially employer) and a small worker (employee).
  - Big workers are denoted as  $m_1, m_2$ , and small ones as  $w_1, w_2$ .
- Suppose that small workers are only productive if they work with the assets they are linked to. We ignore synergies across workers.
- We will study the effect of ownership on small workers' incentives.

- Suppose that we consider two ownership structures: non-integration ( $m_1$  controls  $a_1$  and  $m_2$  controls  $a_2$ ) and type-1 integration ( $m_1$  controls  $a_1$  and  $a_2$ ).
- The FOC for  $w_1$  under non-integration is:

$$\frac{1}{3}v^{w_1}(\{m_1, m_2\}, \{a_1, a_2\}) + \frac{1}{6}v^{w_1}(\{m_1\}, \{a_1\}) = C'_{w_1}(x_{w_1}^e)$$

While under integration it is:

$$\frac{1}{3}v^{w_1}(\{m_1, m_2\}, \{a_1, a_2\}) + \frac{1}{6}v^{w_1}(\{m_1\}, \{a_1, a_2\}) = C'_{w_1}(x_{w_1}^e)$$

Recall that  $w_1$  cares only about coalition with  $a_1$ .

- The FOC for  $w_2$  under non-integration is:

$$\frac{1}{3}v^{w_2}(\{m_1, m_2\}, \{a_1, a_2\}) + \frac{1}{6}v^{w_2}(\{m_2\}, \{a_2\}) = C'_{w_2}(x_{w_2}^e)$$

While under integration it is:

$$\frac{1}{3}v^{w_2}(\{m_1, m_2\}, \{a_1, a_2\}) + \frac{1}{6}v^{w_2}(\{m_1\}, \{a_1, a_2\}) = C'_{w_2}(x_{w_2}^e)$$

- Comparison:

- Type-1 integration is good for  $w_1$ , while for  $w_2$  the effect is ambiguous.

- For  $w_1$ , the productivity of investment is determined only by coalitions with  $a_1$ , which is controlled by  $m_1$ . When  $m_1$  also controls  $a_2$ ,  $w_1$  is getting a boost to productivity when matched with  $m_1$ .
  - This effect represents better **coordination**.
- For  $w_2$ , the better coordination is also present under integration, since whenever he is matched with  $a_2$  he gets a boost to productivity from the presence of  $a_1$ .
- But,  $w_2$  is losing some connection to  $m_2$ , which might be costly.

## Internal Capital Markets

- A different angle on the question of the boundaries of the firm comes from analyzing the optimality of **internal capital markets**.
- Internal capital markets develop when a firm has multiple divisions, potentially in different industries, and transfers resources across divisions. This is what happens in conglomerates.
- The question is what is the benefit from putting various (potentially unrelated) divisions under the same ownership.



## Stein (1997)

- Stein (1997) develops a model, where divisions are constrained in their ability to raise external financing for their projects due to an **agency problem**.
- Having an internal capital market can help mitigating the problem, as the headquarters can raise the financing and allocate them more efficiently across divisions.
- Stein analyzes when this is optimal and sheds light on the trade offs in choosing the size and scope of the internal capital market.

## Basic Setup

- A project started by a *founder* requires a *manager* and a *financier*.
- The amount of investment in the project can be 1 or 2.
- There are two states of the world  $B$  and  $G$ .
- In state  $B$ , investment of 1 yields  $y_1$ , and investment of 2 yields  $y_2$ ,  
where:

$$1 < y_1 < y_2 < 2.$$

Hence, in this state, the optimal investment is 1.

- In state  $G$ , investment of 1 yields  $\theta y_1$ , and investment of 2 yields  $\theta y_2$ , where  $\theta > 1$ , and:

$$\theta(y_2 - y_1) > 1.$$

Hence, in this state, the optimal investment is 2.

- The ex-ante probability of state  $G$  ( $B$ ) is  $p$  ( $1-p$ ).
- The realization is known only to managers, but there is a problem with their incentive to tell the truth as they also receive a non-verifiable private benefit, which is a proportion  $s$  of gross return.

## Credit Rationing

- Eliciting information from managers will be costly when  $s$  is sufficiently large. Then, financiers and founders will have to make decisions without knowing the realization.
- If the amount financed is 1, the expected return is

$$(p\theta + (1 - p))y_1 - 1.$$

- If the amount financed is 2, the expected return is

$$(p\theta + (1 - p))y_2 - 2.$$

- Then, when  $p$  is sufficiently small, investing 1 is more desirable, and this creates **credit rationing**:
  - Credit is rationed in good states of the world because of the lack of ability to convey information.
- As a side, note that compensation contracts could be designed to elicit information.
- However, the cost of eliciting information is  $(1 - p)s(y_2 - y_1)$ , while the benefit is  $p(\theta(y_2 - y_1) - 1)$ , and hence this is not desirable when  $s$  is sufficiently large.

## Corporate Headquarters and the Internal Capital Market

- Suppose that a few projects are grouped together and headquarters raises financing. A few assumptions about corporate headquarters:
  - It can acquire information about projects' prospects.
  - It has no financial resources of its own.
  - It can capture a fraction  $\phi$  of private benefits at the cost of diluting incentives, so that cash flows fall by a fraction  $k < 1$ .
  - It has the authority to redistribute resources across projects.

## **The Role of Headquarters in a Two-Project Example**

- There is no role for headquarters with only one project.
  - There will be reduction in cash flows due to reduced incentives, and no better information revelation since headquarters have the incentives of managers to misreport.
- Suppose there are two uncorrelated projects as described above.
- Suppose that headquarters can perfectly tell their states.
- Suppose that the overall credit constraint is not eased, so that headquarters can raise only 2 for the two projects.

- The potential benefit from the headquarters is its ability to reallocate resources from a project in a bad state to a project in a good state. This is beneficial as long as:

$$\theta(y_2 - y_1) > y_1$$

- Headquarters will have an incentive to do this to maximize private benefits.
- Additional efficiency comes from the headquarters' broader span of control which allows it to derive private benefits from several projects simultaneously.



- Summarizing the trade off:

- The expected net output under external market is:

$$EM = 2(y_1(p\theta + (1 - p)) - 1)$$

- The expected net output under internal market is:

$$IM = 2(1 - p)^2ky_1 + 2p^2k\theta y_1 + 2p(1 - p)k\theta y_2 - 2$$

- By moving to an internal capital market, we sacrifice efficiency at a factor of  $k$ , but in situations where the projects are in different states, we get better allocation of resources.

## Noisy Information and Scope

- A question that often comes up is what is the optimal scope of an internal capital market: How correlated the different divisions should be.
- Stein provides an argument for focus:
  - When information is noisy, headquarters might make mistakes in allocating resources.
  - When the projects are close to each other, noise tends to be correlated, and then relative rankings are not harmed.

## Adjusting the Assumptions

- For each project, headquarters observes information that is either  $H$  (high) or  $L$  (low).
- The informativeness of the signal is captured by  $q$ :

$$\text{prob}(H^i/G^i) = \text{prob}(L^i/B^i) = q, \text{ where } 1/2 < q < 1.$$

- A false low (high) signal in one project makes a false low (high) signal in the other project more likely. This is captured by the parameter  $\alpha$  which summarizes the degree of correlation:

$$\text{prob}(L^i/G^i, G^j, L^j) = (1 - q)(1 + \alpha) > \text{prob}(L^i/G^i) = (1 - q)$$

$$\text{prob}(H^i/B^i, B^j, H^j) = (1 - q)(1 + \alpha) > \text{prob}(H^i/B^i) = (1 - q)$$

- Note that the probability of observing a false (low) signal in what project does not change the probability of observing a false (high) signal in the other project.
- Now, there are 16 possible realizations (2 signals and 2 states for each project).
- Payoffs and probabilities are shown in the following table:

	Outcome/Signal Configuration	Probability	Payoff: External Market	Payoff: Internal Market
1.	GGHH	$p^2(q^2 + \alpha(1 - q)^2)$	$2\theta y_1$	$2\theta y_1$
2.	GBHH	$p(1 - p)q(1 - q)$	$y_1(1 + \theta)$	$y_1(1 + \theta)$
3.	BGHH	$(1 - p)p(1 - q)q$	$y_1(1 + \theta)$	$y_1(1 + \theta)$
4.	BBHH	$(1 - p)^2(1 - q)^2(1 + \alpha)$	$2y_1$	$2y_1$
5.	GGHL	$p^2(q(1 - q) - \alpha(1 - q)^2)$	$2\theta y_1$	$\theta y_2$
6.	GBHL	$p(1 - p)q^2$	$y_1(1 + \theta)$	$\theta y_2$
7.	BGHL	$(1 - p)p(1 - q)^2$	$y_1(1 + \theta)$	$y_2$
8.	BBHL	$(1 - p)^2(q(1 - q) - \alpha(1 - q)^2)$	$2y_1$	$y_2$
9.	GGLH	$p^2(q(1 - q) - \alpha(1 - q)^2)$	$2\theta y_1$	$\theta y_2$
10.	GBLH	$p(1 - p)(1 - q)^2$	$y_1(1 + \theta)$	$y_2$
11.	BGLH	$(1 - p)pq^2$	$y_1(1 + \theta)$	$\theta y_2$
12.	BBLH	$(1 - p)^2(q(1 - q) - \alpha(1 - q)^2)$	$2y_1$	$y_2$
13.	GGLL	$p^2(1 - q)^2(1 + \alpha)$	$2\theta y_1$	$2\theta y_1$
14.	GBLL	$p(1 - p)(1 - q)q$	$y_1(1 + \theta)$	$y_1(1 + \theta)$
15.	BGLL	$(1 - p)pq(1 - q)$	$y_1(1 + \theta)$	$y_1(1 + \theta)$
16.	BLL	$(1 - p)^2(q^2 + \alpha(1 - q)^2)$	$2y_1$	$2y_1$

- The result is that the benefit from an internal capital market increases in the degree of focus  $\alpha$  and that this effect strengthens when  $q$  is smaller.
- The intuition comes from the fact that increasing focus increases the likelihood of configurations like GGHH and BBHH, and lowers the likelihood of configurations like GGHL and BBHL.
- This is good because there is no harm in a configuration like BBHH, as it causes no adverse implications for resource allocation. On the other hand, there is harm in configurations like GGHL and BBHL.