# Trading frenzies and their impact on real investment ☆

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## ARTICLE INFO

## ABSTRACT

We study a model in which a capital provider learns from the price of a firm's security in deciding how much capital to provide for new investment. This feedback effect from the financial market to the investment decision gives rise to trading frenzies, in which speculators all wish to trade like others, generating large pressure on prices. Coordination among speculators is sometimes desirable for price informativeness and investment efficiency, but speculators' incentives push in the opposite direction, so that they coordinate exactly when it is undesirable. We analyze the effect of various market parameters on the likelihood of trading frenzies to arise.

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## 1. Introduction

Trading frenzies in financial markets occur when many speculators rush to trade in the same direction leading to large pressure on prices. Financial economists have long been searching for the sources of trading frenzies, asking what causes strategic complementarities in speculators' behavior. This phenomenon is particularly puzzling given that the price mechanism in financial markets naturally leads to strategic substitutes, whereby the expected change in price caused by speculators' trades makes others want to trade in the opposite direction.[1]

A recent literature develops and analyzes different mechanisms that generate strategic complementarities in

[1] That is, if a speculator expects other speculators to sell a security, then he expects the price of the security to decline, which gives him a reason to buy the security.

financial markets and, hence, could give rise to trading frenzies. An important aspect of real-world trading frenzies that is missing from this literature is their real effect. Firms and regulators are often concerned about a bear raid (i.e., a massive short selling of a stock) because of its implications for the ability of the firm to raise capital and operate. In this paper, we analyze a model in which financial market trading has an effect on the real economy, i.e., on firms' cash flows. Hence, when a trading frenzy arises, it affects not only prices but also firm cash flows, providing a reason for firms to worry and for regulators to intervene. Interestingly, in our model, the real effect itself provides the mechanism for strategic complementarities and trading frenzies to arise.

Intuitively, suppose that speculators in the financial market short sell a stock, leading to a decrease in its price. Because the stock price provides information about the firm's profitability, it affects decisions by various agents, such as capital providers. Seeing the decrease in price, capital providers update downward their expectation of the firm's profitability. This weakens the firm's access to capital and, thus, hurts its performance.[2] As a result, the firm's value decreases, and short sellers are able to make a profit. This creates a source for complementarities, whereby the expected change in value caused by speculators' trades makes others want to trade in the same direction and generates a trading frenzy.

We develop a model to study and analyze this phenomenon. We study an environment where a capital provider decides how much capital to provide to a firm for the purpose of making new real investment. The decision of the capital provider depends on his assessment of the productivity of the proposed investment. In his decision, the capital provider uses two sources of information. His private information and the information aggregated by the price of the firm's security that is traded in the financial market. The reliance of capital provision on financial market prices establishes the effect that the financial market has on the real economy. We refer to this effect as the "feedback effect".[3]

The financial market in our model contains many small speculators trading a security, whose payoff is correlated with the cash flow obtained from the firm's investment. Speculators trade on the basis of information they have about the productivity of the investment. They have access to two signals: the first signal is independent across speculators (conditional on the realization of the productivity), and the second one is correlated among them.[4] The correlated signals introduce common noise in information into the model, which can be due to a rumor, for example. A trading frenzy occurs when speculators put large weight on the correlated signal relative to the idiosyncratic signal, and so they tend to trade similarly to each other.

To close the model, we introduce noisy price-elastic supply in the financial market. The market is cleared at a price for which the demand from speculators equals the supply. The endogenous price, in turn, reflects information about the productivity of the investment, as aggregated from speculators' trades. But, given the structure of information and trading, the information in the price contains noise from two sources: the noisy supply and the common noise in speculators' information. The information in the price is then used by the capital provider, together with his private information, when making the decision about capital provision and investment.

Analyzing the weight speculators put on the correlated signal relative to the idiosyncratic signal, we shed light on the determinants of trading frenzies. In a world with no strategic interactions, this weight is naturally given by the ratio of precisions between the correlated and the idiosyncratic signals. But, in the equilibrium of our model, there are two strategic interactions that shift the weight away from this ratio of precisions. The first effect is the usual outcome of a price mechanism. When speculators put weight on the correlated information, this information gets more strongly reflected in the price, and then the incentive of each individual speculator to put weight on the correlated information decreases. This generates strategic substitutes and pushes the weight that speculators put on the correlated information below the ratio of precisions.[5] The second effect arises due to the feedback effect from the price to the capital provision decision. When speculators put weight on the correlated information, this information gets to have a stronger effect on the capital provision to the firm and, hence, on the real value of its traded security. Then, the incentive of each speculator to put weight on this information increases. This leads to strategic complementarities that make speculators put a larger weight on the correlated signal.

This second effect is what causes a trading frenzy, leading speculators to put large weight on their correlated information and to trade in a coordinated fashion. When this effect dominates, our model generates a pattern that looks like a run on a stock by many speculators, who are driven by common noise in their correlated signals (e.g., rumor), leading to a price decline, lack of provision of new capital, and collapse of real value. This echoes some highly publicized events such as the bear raid on Overstock.com in 2005 or the bear raids on Bear Stearns and Lehman Brothers in 2008.[6]

Our model provides testable predictions that can guide future empirical work. The main feature of our model is the connection between trading frenzies, which are episodes of large buying or selling pressure, and real

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[2] Other agents who could be affected by the information in the price are managers, employees, customers, etc.

[3] In our model, the financial market is a secondary market and, hence, the only feedback from it to the firm's cash flow is informational. There is no transfer of cash from the market to the firm.

[4] In our model, the correlation is perfect, but this is not essential.

[5] Strategic substitutes due to the price mechanism appear in various forms in the literature on financial markets. See, for example, Grossman and Stiglitz (1980).

[6] Our model also generates a similar pattern in the other direction. Many speculators buy the stock, leading to a price increase, provision of more new capital, and increase in real value (in the case in which the firm was financially constrained). This resembles events such as the Internet boom in the late 1990s or the real estate boom that preceded the recent crisis.

variables, such as credit and cash available to the firm. This connection is double-sided. First, a trading frenzy has a spillover to the firm's credit, investment, and cash flow due to the information inferred from the price by capital providers. Second, the reliance of the firm's cash flows on prices is the source of the strategic complementarity in trading that gives rise to the trading frenzy. We provide suggestive evidence that is consistent with these forces in our model. However, there is room for a thorough empirical study to follow up on our paper and demonstrate the connection between trading frenzies and real variables with a careful identification strategy.

Using comparative statics analysis, we also investigate theoretically other factors that affect the likelihood of trading frenzies. This analysis provides additional ground for future empirical work. First, we show that, in our model, speculators are more likely to trade in a coordinated fashion when the supply in the financial market is more elastic with respect to the price. This can be interpreted as a more liquid market. In such a market, the strategic substitutes due to the price mechanism are weak, as informed demand is easily absorbed by the elastic supply without having much of a price impact. Hence, speculators tend to put more weight on correlated information and trade more similarly to each other. Empirically, the elasticity of supply with respect to the price can be captured by traditional liquidity measures, such as the inverse of the sensitivity of price to order flow (see Amihud, 2002, for an empirical implementation).

Second, we find that, in our model, when there is small variance in the supply function, i.e., when there is small variance in noise (liquidity) trading in the financial market, speculators tend to put large weights on their correlated signals and, thus, to act in a coordinated fashion. This is because, in these situations, the capital provider relies more on the information in the price since the price is less noisy and so the feedback effect from the market to the firm's cash flows strengthens, increasing the scope of strategic complementarities. Capturing the variance in noise/liquidity trading empirically is challenging. One way to think about this is to classify different types of traders based on the extent to which they are prone to liquidity shocks. For example, mutual funds are more prone to liquidity shocks than hedge funds (given that the latter have stronger restrictions on redemptions). Then, stocks held primarily by hedge funds have lower variance of noise (liquidity) trading than stocks held primarily by mutual funds.

Third, the precision of various sources of information also plays an important role in shaping the incentive to rely on correlated versus uncorrelated information. Intuitively, more coordination exists when speculators' correlated signals are sharper and when their uncorrelated signals are noisier. Interestingly, there is more coordination when the capital provider has less precise information of his own, as then the feedback from the market to his decision is stronger. For empirical testing, one can think of information precisions changing across firms based on their type of business. For example, following the rationale in Luo (2005), one can expect that in technology firms the capital provider, who is closer to

the firm than market participants, has an informational advantage over the market, whereas the market has an informational advantage for firms when the uncertainty revolves mostly around the demand for products. Assessing the precision of common market information versus private speculators' information is more challenging. One can potentially look at the extent to which speculators exchange information about a stock over the Internet as indication for the extent to which they are exposed to common information.

Another question we ask is whether trading frenzies are good or bad for the efficiency of the capital provision decision. We find that they are sometimes good and sometimes bad and that a conflict arises between the level of coordination in equilibrium and the one that maximizes the efficiency of the capital provision decision. The efficiency of the capital provision decision is maximized when the informativeness of the price is highest. It turns out that when there is high variance of noise (liquidity) trading in the market, higher degree of coordination among speculators increases price informativeness. This is because, in noisy markets, coordination among speculators is beneficial in suppressing the noise in liquidity trading that reduces the informativeness of the price. In such markets, trading frenzies among speculators are desirable because they enable decision makers to detect some trace of informed trading in a market subject to large volume of liquidity trading and noise. However, when the market is less noisy, the importance of coordination among speculators declines, and the additional noise that coordination adds via the excess weight that speculators put on their correlated information (which translates into weight on common noise) makes coordination undesirable. Hence, the conflict arises because high levels of coordination are desirable in noisy markets, but in equilibrium, speculators coordinate more in less noisy markets.

This analysis can provide a basis for policy discussions regarding the role of financial markets in the economy and potential ways to regulate them. Regulatory agencies, such as the Securities and Exchange Commission (SEC), are often concerned about the damaging effect of speculative trading, and calls are often made for intervention in speculative markets. However, it is hard to justify such interventions in models in which the financial market is a side show and does not have a feedback effect on the real economy. As we show, trading patterns in the financial market have an effect on the efficiency of real investment, and so this could provide a reason for intervention in financial market trading. We argue that imposing limits on speculation might not be wise due to the direct negative effect this has on price informativeness and investment efficiency. However, more sophisticated intervention involving changes in market liquidity can alter the incentives of speculators to coordinate and improve price informativeness and investment efficiency.

The remainder of this paper is organized as follows. Section 2 discusses related literature and empirical motivation for our model. In Section 3, we present the model setup and characterize the equilibrium of the model. In Section 4, we solve the model. Section 5 analyzes the

determinants of coordination among speculators in our model. In Section 6, we discuss the implications for the efficiency of investments and the volatility of prices and investments. Section 7 concludes. All proofs are provided in the Appendix.

## 2. Literature review and empirical motivation

The existing literature offers theoretical models with strategic complementarities in financial markets generating excess volatility in trading and prices. Papers in this literature include Froot, Scharfstein, and Stein (1992), Hirshleifer, Subrahmanyam, and Titman (1994), Veldkamp (2006a, 2006b), Ganguli and Yang (2009), Amador and Weill (2010), and Garcia and Strobl (2011). In these papers, strategic complementarities are in the decision on information acquisition, i.e., due to various mechanisms, speculators produce more information when other speculators produce more information. Excess volatility in prices has also been generated due to learning from the price by speculators in the financial market, e.g., in Barlevy and Veronesi (2003), Hassan and Mertens (2011), and Breon-Drish (2012). In these models, a decrease in price can be amplified as speculators interpret it as bad news about the asset and so increase their selling pressure.

The main feature that distinguishes our model from all the models mentioned above is the connection between trading in the financial market and the decisions made in the real side of the economy. This connection is double-sided. First, a trading frenzy, when speculators rush to trade in the same direction, has a spillover to the firm's investment and cash flow due to the information inferred from the price by capital providers. Second, the reliance of the firm's cash flows on prices is the source of the strategic complementarity in trading that gives rise to the trading frenzy. Anecdotal and large-sample empirical evidence suggest that the connection to the real side is a very pertinent component of trading frenzies.

Anecdotally, when firms are attacked by short sellers, their main concern is about the effect that this will have on their cash flows and operations. For example, Overstock.com, which was subject to a large short-selling attack in 2005, subsequently sued a few large traders, noting the real damage that the attack has caused to the firm's operations. The following quote from the lawsuit demonstrates this concern: "Defendants' concerted and wrongful actions have resulted in substantial harm to Overstock. Among the harms defendants' actions have caused Overstock are: harm to Overstock's reputation and good will, loss of product sales and the profits therefrom; interference with and damage to Overstock's relationships with its suppliers, bankers, lenders, institutional investors, and the media; loss of market share and business opportunity for its products; increased cost to Overstock in its acquisition of SkiWest, Inc; loss of investment capital; loss of operating capital and impairment of Overstock's ability to continue to grow at historical rates".[7]

Overstock's available cash and its short-term debt were cut by about half over the year following the short-selling attack, reflecting the difficulty in rolling over the debt and maintaining cash positions.

The two more recent cases of Bear Stearns and Lehman Brothers are also well known for their real effect. Both firms depended heavily on the rollover of short-term debt, and a decrease in stock price had the potential to harm their ability to rollover their debt and so hurt their operations. After mounting selling pressure in the financial market, Bear Stearns was close to bankruptcy in March 2008, leading to a bail out by the government and acquisition by JPMorgan Chase. Lehman Brothers went bankrupt in September 2008 after mounting selling pressure for its equity traded in the stock market. The SEC imposed a short sales ban for stocks of financial firms in 2008, noting that "financial institutions are particularly vulnerable… because they depend on the confidence of their trading counterparties in the conduct of their core business".[8]

Basic data analysis reveals that the connection between trading frenzies and firms' operations holds more systematically. We use the Regulation SHO database, which contains all short sales reported to NYSE for NYSE-listed securities from January 2005 to June 2007. The database was compiled for an SEC pilot program to amend the uptick rule, during which period broker dealers were required to mark the trades as either long or short. The data set contains all intraday short sales executed on NYSE during the 30-month period. We merge the data set with the CRSP to obtain returns and trading volume, and with Compustat to obtain fundamental variables. Some stocks are dropped during the merging process, and the final data set contains 2271 unique securities and is fairly representative of the overall market.

For each stock and every trading week, we calculate the total number of shares reported as short sales and then obtain the total trading volume for the stock from CRSP. We calculate the short ratio as the ratio of the weekly trading volume that is sold short. We define stocks that are subject to a bear raid as stocks that are above the 95th percentile in short ratio and followed by negative return response in the following week. We compare the behavior and characteristics of raided stocks with the behavior and characteristics of other stocks.

First, we look at the dependence of the firm on short-term funding. When a firm depends more heavily on short-term funding, it is more sensitive to price changes in the financial market and so the feedback effect is stronger, which according to our model should give rise to stronger strategic complementarities and trading frenzies. We capture the dependence of the firm on short-term funding as the ratio between the firm's current debt and its current assets, with current debt defined as the sum of short-term debt and long-term debt that is due in less than one year. Consistent with our theory, we find that

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raided firms are much more dependent on short-term funding than other firms. The average ratio of current debt to current assets is 20.77% among raided firms and only 13.54% in the overall sample. These results are significant at less than the 1% level.

Second, we look at what happens to the firm following a short-selling attack. In particular, we look at changes in cash, in current debt, and in operating earnings in the quarter following a bear raid and compare them with the average experience of firms in the sample. Our theory suggests that, due to the feedback effect, firms that are subject to a short-selling attack have a hard time rolling over their debt and so experience a decrease in their current debt, leading to a decrease in cash and ultimately hurting their operating earnings. The evidence is consistent with this story. During the quarter following a bear raid, a firm's cash decreases on average by $53.5 million, and in the overall sample firms experience an average increase of $84.3 million in cash per quarter. Similarly, in the quarter following a bear raid, current debt decreases by $105 million (compared with an average quarterly increase of $107.6 million in current debt in the overall sample), and operating earnings decrease by $1.74 per share (compared with an average quarterly decrease of $0.01 in operating earnings per share in the overall sample). These results are significant at less than the 1% level.

Overall, both anecdotal and large-sample empirical evidence suggests that the feedback loop between firms' operations and the trading of their stocks is an important element in the emergence of trading frenzies. This element is the focus of our model, and it distinguishes our model from other theories of strategic complementarities in trading leading to trading frenzies. Clearly, the evidence presented here is only suggestive. There is room for a thorough empirical study that considers identification issues. To the best of our knowledge, no empirical study in the existing literature looks at the connection between trading frenzies and the real operations of the firm. We hope that our model with its many predictions and the suggestive empirical evidence presented here will stimulate such empirical research.

Our paper contributes to a growing literature on the feedback effect from trading in financial markets to corporate decisions based on the informational content of market prices. The basic motivation for this literature goes back to Hayek (1945), who posits that market prices provide an important source of information for various decision makers. A number of papers provide empirical evidence for this link. Luo (2005) shows that an abnormal decrease in stock price following an acquisition announcement increases the likelihood that the acquisition will be cancelled and that this effect is stronger in cases in which the acquirer has more to learn from the market. Chen, Goldstein, and Jiang (2007) show that the sensitivity of corporate investment to market price is stronger when the market price contains more information (based on microstructure measures of price informativeness) that is not otherwise available to firm managers. On the theoretical side, papers in this literature include Fishman and Hagerty (1992), Leland (1992), Khanna, Slezak, and Bradley

(1994), Boot and Thakor (1997), Dow and Gorton (1997), Subrahmanyam and Titman (1999), Fulghieri and Lukin (2001), Bond, Goldstein, and Prescott (2010), and Kurlat and Veldkamp (2012).

Several recent papers in this literature are more closely related to the mechanism in our paper. Ozdenoren and Yuan (2008) show that the feedback effect from asset prices to the real value of a firm generates strategic complementarities. In their paper, however, the feedback effect is modeled exogenously and is not based on learning. As a result, their paper does not deliver the implications that our paper delivers on the effect of liquidity and various information variables on coordination and efficiency. Khanna and Sonti (2004) also model feedback exogenously and show how a single trader can increase the value of his existing inventory in the stock by trading to affect the value of the firm. Goldstein and Guembel (2008) do analyze learning by a decision maker and show that this might lead to manipulation of the price by a single potentially informed trader. Hence, the manipulation equilibrium in their paper is not a result of strategic complementarities among heterogeneously informed traders.[9] Hirshleifer, Subrahmanyam, and Titman (2006) also analyze learning by a decision maker, and show that the feedback effect enables irrational traders who trade on common noise to make a profit. However, in their model, the decision of these traders to trade on noise is exogenous (they act irrationally) and is not endogenized as a result of a coordination problem. Dow, Goldstein, and Guembel (2007) show that the feedback effect generates complementarities in the decision to produce information, but not in the trading decision.

Our paper is most closely related to Goldstein, Ozdenoren, and Yuan (2011) and Angeletos, Lorenzoni, Pavan (2010). Both of these papers derive endogenous complementarities as a result of learning from the aggregate action of agents. To analyze trading frenzies and their impact on real investments, we embed this mechanism in a model of financial markets in which a capital provider learns from the price to make an investment decision. Modeling the financial market explicitly enriches the problem in various ways. For example, having a price mechanism introduces strategic substitutes that coexist with the strategic complementarities in the model.[10] Hence, our model is substantially different from the above mentioned models. In terms of results, our model generates new insights in the context of our study, such as the effect of supply elasticity and noise trading on coordination in financial markets. We also derive new results on the difference between the equilibrium level of coordination and the efficient level of coordination.

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[9] More recently, Khanna and Mathews (2012) extend the model by Goldstein and Guembel (2008) to allow for the presence of a blockholder as in Khanna and Sonti (2004) and study when manipulation occurs in spite of the presence of a blockholder who tries to maximize firm value.

[10] Another technical detail that we highlight in the description of the model is the use of log-normal distributions, which is necessary in a setting of feedback from financial market prices to investment decisions.

## 3. Model

The model has one firm and a traded asset. A capital provider has to decide how much capital to provide to the firm for the purpose of making an investment. There are three dates, $t=0,1,2$. At date 0, speculators trade in the asset market based on their information about the fundamentals of the firm. At date 1, after observing the asset price and receiving private information, the capital provider of the firm decides how much capital the firm can have and the firm undertakes investment accordingly. Finally, at date 2, the cash flow is realized and agents get paid.

### 3.1. Investment

The firm in this economy has access to a production technology, which at time $t=2$ generates cash flow $\tilde{F}I$. Here, $I$ is the amount of investment financed by the capital provider, and $\tilde{F} \geq 0$ is the level of productivity. Let $\tilde{f}$ denote the natural log of productivity, $\tilde{f} = \ln \tilde{F}$. We assume that $\tilde{f}$ is unobservable and drawn from a normal distribution with mean $\bar{f}$ and variance $\sigma_f^2$. We use $\tau_f$ to denote $1/\sigma_f^2$. Assuming a log-normal distribution for the productivity shock $\tilde{F}$ enables us to get a tractable closed-form solution.

At time $t=1$ the capital provider chooses the level of capital $I$. Providing capital is costly and the capital provider must incur a private nonpecuniary cost of $C(I) = \frac{1}{2}cI^2$, where $c > 0$. This cost can be thought of as the cost of raising the capital, which is increasing in the amount of capital provided, or as effort incurred in monitoring the investment, which is also increasing in the size of the investment. The capital provider's benefit increases in the cash flow generated by the investment. To ease the exposition, we assume that he captures proportion $\beta \in (0,1)$ of the full amount and, thus, his payoff from the investment is $\beta \tilde{F}I$. The capital provider chooses $I$ to maximize the value he captures from the cash flow generated by the firm's production technology minus his cost of raising capital $C(I)$, conditional on his information set, $\mathcal{F}_l$, at $t=1$:

$$I = \arg \max_I E[\beta \tilde{F}I - C(I)|\mathcal{F}_l]. \tag{1}$$

The solution to this maximization problem is

$$I = \frac{\beta E[\tilde{F}|\mathcal{F}_l]}{c}. \tag{2}$$

The capital provider's information set, denoted by $\mathcal{F}_l$, consists of a private signal $\tilde{s}_l$ and the asset price $P$ observed at date 0. That is, $\mathcal{F}_l = \{\tilde{s}_l, P\}$. The private signal $\tilde{s}_l$ is a noisy signal about $\tilde{f}$ with precision $\tau_l$: $\tilde{s}_l = \tilde{f} + \sigma_l \tilde{\epsilon}_l$, where $\tilde{\epsilon}_l$ is distributed normally with mean zero and standard deviation of 1 and $\tau_l = 1/\sigma_l^2$. Later, we conduct comparative statics with respect to the precision of the capital provider's private signal. It is important to emphasize that even though our capital provider learns from the information in the price, he still could have good sources of private information. In fact, his signal can be more precise than other signals in the economy. Despite this, he still attempts to learn from the market, as agents in the market have other signals that are aggregated by the price.

### 3.2. Speculative trading

The traded asset is a claim on $(1-\beta)\tilde{F}I$, the cash flow that remains after removing the capital provider's share. This is realized at the final date $t=2$. The price of this risky asset at $t=0$ is denoted by $P$. In Section 4.1, we discuss the nature of the traded asset and compare it with alternatives. Because the cost of the investment $C(I)$ is a private non-pecuniary cost incurred by the capital provider, our traded asset can be viewed as equity.[11]

The value of the traded asset here increases in the firm's investment. This is a typical feature of equity in a financially constrained firm, where equity holders would like to see more capital invested in their firm but are constrained in how much capital they can raise, due to additional costs borne by capital providers. Hence, our model is suitable to explain trading frenzies and their real impact in such firms. Our motivating examples, discussed in the Introduction and in Section 2, involve financially constrained firms.[12]

In the market, there is a measure-one continuum of heterogeneously informed risk-neutral speculators indexed by $i \in [0, 1]$. Each speculator is endowed with two signals about $\tilde{f}$ at time 0. The first signal, $\tilde{s}_i = \tilde{f} + \sigma_s \tilde{\epsilon}_i$, is privately observed where $\tilde{\epsilon}_i$ is independently normally distributed across speculators with mean zero and unit variance. The precision of this signal is denoted as $\tau_s = 1/\sigma_s^2$. The second signal is $\tilde{s}_c = \tilde{f} + \sigma_c \tilde{\epsilon}_c$. This signal is observed by all speculators and $\tilde{\epsilon}_c$ is independently and normally distributed with mean zero and unit variance and $\tau_c = 1/\sigma_c^2$.[13]

Each speculator can buy or sell up to a unit of the risky asset. The size of speculator $i$'s position is denoted by $x(i) \in [-1, 1]$. This position limit can be justified by limited capital or borrowing constraints faced by speculators.[14] Due to risk neutrality, speculators choose their positions to maximize expected profits. A speculator's profit from shorting one unit of the asset is given by $P - (1-\beta)\tilde{F}I$, where $(1-\beta)\tilde{F}I$ is the asset payoff and $P$ is the price of the asset. Similarly, a speculator's profit from buying one unit of the asset is given by $(1-\beta)\tilde{F}I - P$.

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[11] Alternatively, the traded asset can be thought of as a derivative whose payoff is tied to the return from the investment.

[12] No matter what the nature of the asset is, our market is a secondary market with no cash transfers to the firm. The only effect of the market on the firm is via the information revealed in the trading process.

[13] The assumption that the second signal is a common signal greatly simplifies the analysis. However, it is not necessary. The necessary element is that the noise in the information observed by speculators has a common component that cannot be fully teased out by the capital provider. In Goldstein, Ozdenoren, and Yuan (2011), we analyze an alternative setup, in which the second signal is specified as a heterogenous private signal with a common noise component $\tilde{\epsilon}_c$ and an agent-specific noise component $\tilde{\epsilon}_{2i}$. That is, $\tilde{s}_{ci} = \tilde{f} + \sigma_c \tilde{\epsilon}_c + \sigma_{c2}\tilde{\epsilon}_{2i}$, where $\tilde{\epsilon}_c$ and $\tilde{\epsilon}_{2i}$ are independently normally distributed variables with mean zero and variance one. That paper, however, was simpler on other dimensions, as there was no price formation for the traded asset.

[14] The specific size of this position limit on asset holdings is not crucial for our results. What is crucial is that informed speculators cannot take unlimited positions, if they do, strategic interaction among informed speculators becomes immaterial.

Formally, speculator $i$ chooses $x(i)$ to solve

$$\max_{x(i)\in[-1,1]} x(i)E[(1-\beta)\tilde{F}I-P|\mathcal{F}_i], \qquad (3)$$

where $\mathcal{F}_i$ denotes the information set of speculator $i$ and consists of $\tilde{s}_i$ and $\tilde{s}_c$. Because each speculator has measure zero and is risk neutral, an informed speculator optimally chooses to either short up to the position limit or buy up to the position limit. We denote the aggregate demand by speculators as $X = \int_0^1 x(i)\,di$, which is given by the fraction of speculators who buy the asset minus the fraction of those who short the asset. We assume that speculators do not observe the price when they trade and, hence they submit market orders, as in Kyle (1985). This setup of the financial market is a simple way to capture the (important) idea that speculators, when they trade, do not have the market information that the capital provider has when making the lending or investment decision later on (the capital provider bases the investment decision on the price of the security). One could capture this idea in a more complicated dynamic framework, where the capital provider observes prices from multiple rounds of trade and speculators observe only current and past prices. However, such settings only complicate the model, leading to loss of tractability, without adding much economic insight.

### 3.3. Market clearing

At date 0, conditional on his information, each speculator submits a market order to buy or sell a unit of the asset to a Walrasian auctioneer. The Walrasian auctioneer then obtains the aggregate demand by speculators $X$ and also a noisy supply curve from uninformed traders and sets a price to clear the market. The noisy supply of the risky asset is exogenously given by $Q(\tilde{\xi},P)$, a continuous function of an exogenous demand shock $\tilde{\xi}$ and the price $P$. The supply curve $Q(\tilde{\xi},P)$ is strictly decreasing in $\tilde{\xi}$ and increasing in $P$; that is, it is upward sloping in price. The demand shock $\tilde{\xi}\in\mathbb{R}$ is independent of other shocks in the economy, and $\tilde{\xi}\sim N(0,\sigma_\xi^2)$. As always, we denote $\tau_\xi = 1/\sigma_\xi^2$.

The usual interpretation of noisy supply or demand is that there are agents who trade for exogenous reasons, such as liquidity or hedging needs. They are usually referred to as "noise traders." Several papers in the finance literature have explicitly endogenized the actions of these traders in simpler settings, but doing so here significantly complicates the model. One possibility is that the scale of noise trading depends on the amount of information available in the market. In additional analysis we conducted, we show that allowing noise trading to depend on the informational parameters of our model (the precisions of the different signals) does not change our results.[15] In future work, it will be interesting to endogenize noise trading more fully, understanding how their presence is affected by the potential for trading frenzies. In this paper, we derive comparative statics only in the other direction, analyzing the effect of the amount of noise trading in the market (captured by $\sigma_\xi^2$) on the likelihood and desirability of trading frenzies.

To solve the model in closed form, we assume that $Q(\tilde{\xi},P)$ takes the following functional form:

$$Q(\xi,P) = 1-2\Phi(\tilde{\xi}-\alpha\ln P), \qquad (4)$$

where $\Phi(\cdot)$ denotes the cumulative standard normal distribution function. The parameter $\alpha$ captures the elasticity of the supply curve with respect to the price. It can be interpreted as the liquidity of the market. When $\alpha$ is high, the supply is very elastic with respect to the price, and so large informed demand is easily absorbed in the price without having much of a price impact. This notion of liquidity is similar to that in Kyle (1985), where liquidity is considered high when the informed trader has a low price impact. The basic features assumed in (4), i.e., that the supply is increasing in price and also has a noisy component, are standard in the literature. It is also common in the literature to assume particular functional forms to obtain tractability. The specific functional form assumed here is close to that in Dasgupta (2007) and Hellwig, Mukherji, and Tsyvinski (2006).

### 3.4. Equilibrium

We now turn to the definition of equilibrium.

*Definition 1.* An equilibrium consists of a price function, $P(\tilde{f},\tilde{e}_c,\tilde{\xi}) : \mathbb{R}^3 \to \mathbb{R}$, an investment policy for the capital provider $I(\tilde{s}_l,P) : \mathbb{R}^2 \to \mathbb{R}$, strategies for speculators, $x(\tilde{s}_i,\tilde{s}_c) : \mathbb{R}^2 \to [-1,1]$, and the corresponding aggregate demand $X(\tilde{f},\tilde{e}_c)$, such that

- for speculator $i$, $x(\tilde{s}_i,\tilde{s}_c)\in\arg\max_{x(i)\in[-1,1]}x(i)E[(1-\beta)\tilde{F}I-P|\tilde{s}_i,\tilde{s}_c]$;
- the capital provider's investment is $I(\tilde{s}_l,P) = \beta E[\tilde{F}|\tilde{s}_l,P]/c$; and
- the market clearing condition for the risky asset is satisfied:

$$Q(\tilde{\xi},P) = X(\tilde{f},\tilde{e}_c)\equiv \int x(\tilde{f}+\sigma_s\tilde{e}_i,\tilde{f}+\sigma_c\tilde{e}_c)\,d\Phi(\tilde{e}_i). \qquad (5)$$

*Definition 2.* A *linear monotone equilibrium* is an equilibrium in which $x(\tilde{s}_i,\tilde{s}_c) = 1$ if $\tilde{s}_i + k\tilde{s}_c\geq g$ for constants $k$ and $g$, and $x(\tilde{s}_i,\tilde{s}_c) = -1$ otherwise.

In words: in a linear monotone equilibrium, a speculator buys the asset if and only if a linear combination of his signals is above a cutoff $g$ and sells it otherwise. In the rest of the paper we focus on linear monotone equilibria.

## 4. Solving the model

In this section, we explain the main steps that are required to solve our model. Restricting attention to a linear monotone equilibrium, we first use the market clearing condition to determine the asset price. We then characterize the information content of the asset price to derive the capital provider's belief on $\tilde{f}$ based on $\{P,\tilde{s}_l\}$ and solve for the optimal investment problem. Finally, given the capital provider's investment rule and the asset pricing rule, we solve for individual speculators' optimal trading decision.

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[15] Details are available upon request.

In a linear monotone equilibrium, speculators short the asset whenever $\tilde{s}_i + k\tilde{s}_c \leq g$ or, equivalently, $\sigma_s \tilde{\epsilon}_i \leq g - (1 + k)\tilde{f} - k\sigma_c \tilde{\epsilon}_c$. Hence, their aggregate selling can be characterized by $\Phi((g - (1 + k)\tilde{f} - k\sigma_c\tilde{\epsilon}_c)/\sigma_s)$. Conversely, they purchase the asset whenever $\tilde{s}_i + k\tilde{s}_c \geq g$ or, equivalently, $\sigma_s\tilde{\epsilon}_i \geq g - (1 + k)\tilde{f} - k\sigma_c\tilde{\epsilon}_c$. Hence, their aggregate purchase can be characterized by $1 - \Phi((g - (1 + k)\tilde{f} - k\sigma_c\tilde{\epsilon}_c)/\sigma_s)$. The net holding from speculators is then

$$X(\tilde{f}, \tilde{\epsilon}_c) = 1 - 2\Phi\left(\frac{g - (1 + k)\tilde{f} - k\sigma_c\tilde{\epsilon}_c}{\sigma_s}\right). \tag{6}$$

The market clearing condition together with Eq. (4) indicate that

$$1 - 2\Phi\left(\frac{g - (1 + k)\tilde{f} - k\sigma_c\tilde{\epsilon}_c}{\sigma_s}\right) = 1 - 2\Phi(\tilde{\xi} - \alpha \ln P). \tag{7}$$

Therefore, the equilibrium price is given by

$$P = \exp\left(\frac{(1 + k)\tilde{f} + k\sigma_c\tilde{\epsilon}_c - g + \sigma_s\tilde{\xi}}{\alpha\sigma_s}\right) = \exp\left(\frac{\tilde{f} + k\tilde{s}_c - g + \sigma_s\tilde{\xi}}{\alpha\sigma_s}\right), \tag{8}$$

which is informationally equivalent to

$$z(P) \equiv \frac{g + \alpha\sigma_s \ln P}{1 + k} = \tilde{f} + \frac{k}{1 + k}\sigma_c\tilde{\epsilon}_c + \frac{1}{1 + k}\sigma_s\tilde{\xi}$$
$$= \left(\frac{1}{1 + k}\right)\tilde{f} + \frac{k}{1 + k}\tilde{s}_c + \frac{1}{1 + k}\sigma_s\tilde{\xi}. \tag{9}$$

From Eq. (9), $z(P)$, which is a sufficient statistic for the information in $P$, provides some information about the realization of the productivity shock $\tilde{f}$. Yet, the signal $z(P)$ is not fully revealing of $\tilde{f}$, as it is also affected by the noise in the common signal $\tilde{\epsilon}_c$ and by the noisy demand $\tilde{\xi}$. Because the capital provider observes $z(P)$, he uses it to update his belief about the productivity. The statistic $z(P)$ is distributed normally with a mean of $\bar{f}$. The variance of $z(P)$ given $\tilde{f}$ is $\sigma_p^2 = (k/(1 + k))^2\sigma_c^2 + (1/(1 + k))^2\sigma_s^2\sigma_\xi^2$. Hence, we denote the precision of $z(P)$ as a signal for $\tilde{f}$ as

$$\tau_p = 1/\sigma_p^2 = \frac{(1 + k)^2\tau_c\tau_\xi\tau_s}{k^2\tau_\xi\tau_s + \tau_c}. \tag{10}$$

After characterizing the information content of the price, we can derive the capital provider's belief on $\tilde{f}$. That is, conditional on observing $\tilde{s}_l$ and $z(P)$, the capital provider believes that $\tilde{f}$ is distributed normally with mean $(\tau_f\bar{f} + \tau_l\tilde{s}_l + \tau_p z(P))/(\tau_f + \tau_l + \tau_p)$ and variance $1/(\tau_f + \tau_l + \tau_p)$. Then, using the capital provider's investment rule in Eq. (1) and taking expectations, we can express the level of investment as

$$I = \frac{\beta}{c}E[\tilde{F}|\tilde{s}_l = s_l, P] = \frac{\beta}{c}E[\exp(\tilde{f})|\tilde{s}_l = s_l, P]$$
$$= \frac{\beta}{c}\exp\left(\frac{\tau_f\bar{f} + \tau_l s_l + \tau_p z(P)}{\tau_f + \tau_l + \tau_p} + \frac{1}{2(\tau_f + \tau_l + \tau_p)}\right). \tag{11}$$

Given the capital provider's investment policy in Eq. (11) and the price in Eq. (8), we can now write speculator $i$'s expected profit from buying the asset given the information that is available to him (shorting the asset

would give the negative of this):

$$E[(1-\beta)\tilde{F}I - P|\tilde{s}_i, \tilde{s}_c] = \frac{\beta(1-\beta)}{c}E\left[\exp\left(\frac{\tau_f\bar{f} + \tau_l s_l + \tau_p z(P)}{\tau_f + \tau_l + \tau_p}\right.\right.$$
$$\left.\left. + \frac{1}{2(\tau_f + \tau_l + \tau_p)} + \tilde{f}\right)\bigg|\tilde{s}_i, \tilde{s}_c\right]$$
$$- E\left[\exp\left(\frac{\tilde{f} + k\tilde{s}_c - g + \sigma_s\tilde{\xi}}{\alpha\sigma_s}\right)\bigg|\tilde{s}_i, \tilde{s}_c\right]. \tag{12}$$

We make use here of the fact that $\tilde{F} = \exp(\tilde{f})$. This is where using the natural log of the productivity parameter plays a key role. Using the properties of the exponential function, we can express the value of the firm $\tilde{F}I$ as $(\beta(1-\beta)/c)\exp(\cdot)$, where the expression in parentheses is linear in $\tilde{f}$. This enables us to get a linear closed-form solution, which would otherwise be impossible in a model of feedback.

Conditional on observing $\tilde{s}_i$ and $\tilde{s}_c$, speculator $i$ believes that $\tilde{f}$ is distributed normally with mean $(\tau_f\bar{f} + \tau_s\tilde{s}_i + \tau_c\tilde{s}_c)/(\tau_f + \tau_s + \tau_c)$ and variance $1/(\tau_f + \tau_s + \tau_c)$. Hence, substituting for $z(P)$ [from Eq. (9)] and taking expectations, Eq. (12) can be rewritten as

$$E[(1-\beta)\tilde{F}I - P|\tilde{s}_i, \tilde{s}_c] = \frac{\beta(1-\beta)}{c}\exp(a_0 + a_1\tilde{s}_i + a_2\tilde{s}_c)$$
$$- \exp(b_0 + b_1\tilde{s}_i + b_2\tilde{s}_c), \tag{13}$$

where the coefficients $a_0$, $a_1$, $a_2$, $b_0$, $b_1$, and $b_2$ are functions of $k$ and of the model's parameters. Explicit expressions for these coefficients are provided in the proof of Proposition 1 in the Appendix.

A speculator chooses to buy the asset if and only if Eq. (13) is positive. Rearranging and taking logs leads to the following condition:

$$\tilde{s}_i + B(k)\tilde{s}_c \geq C(k), \tag{14}$$

where $B(k) = (a_2 - b_2)/(a_1 - b_1)$ and $C(k) = (b_0 - a_0 + \ln(c/\beta(1-\beta)))/(a_1 - b_1)$.[16] Function $B(k)$ can be thought of as the best response of a speculator to other speculators' weight on the correlated signal. That is, if all speculators in the economy put a relative weight $k$ on the correlated signal when deciding whether to attack or not, the best response for a speculator is to put the weight $B(k)$ on his correlated signal. The symmetric equilibrium is solved when $B(k) = k$. Coefficients $a_1$, $a_2$, $b_1$, and $b_2$ are also functions of $k$ and, hence, the equilibrium condition $B(k) = k$ leads to a third-order polynomial. Analyzing this polynomial, we obtain the result in Proposition 1. All proofs are in the Appendix.

*Proposition 1. For a high enough level of supply elasticity $\alpha$, there exists a linear monotone equilibrium characterized by weight $k^* > 0$ that speculators put on the common signal. This equilibrium is unique when the precision of the prior $\tau_f$ is sufficiently small.*

The weight $k^*$ that speculators put on the common signal in equilibrium captures the degree of coordination in their trading decisions. When $k^*$ is high, speculators put a large weight on the common information when deciding whether to sell or buy the asset. This leads to large

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[16] Here, we assume that $a_1 - b_1 > 0$. This is verified later in the proof of Proposition 1.

coordination among them and gives rise to a trading frenzy. In Section 5, we develop a series of results on the determinants of coordination and its implications for the efficiency of the investment decision and for the volatility of prices. We focus on the case of large supply elasticity (large $\alpha$) and imprecise prior (small $\tau_f$), for which we know that there exists a unique equilibrium.

### 4.1. A note on the nature of the traded security

Our model assumes that the traded security is a claim on some portion of the cash flow from the investment $\tilde{F}I$. This can be interpreted as equity of the traded firm, in case the firm is financially constrained, or as a derivative.

The key feature of the traded security is that its cash flow depends not only on the fundamental $\tilde{F}$, but also on the investment decision $I$. This introduces a feedback loop between the financial market and the real economy, whereby the price affects the investment decision, and the investment decision is reflected in the price. This feedback loop is the crucial element for our result on strategic complementarities and trading frenzies. To illustrate this, note that if the traded security was a claim on the fundamental $\tilde{F}$, there would be no feedback loop and no frenzies. When speculators trade on $\tilde{F}$, the value of the security is exogenous and, hence, does not depend on speculators' behavior. This eliminates the strategic interaction that is central to our paper. A security on $\tilde{F}$ might also not be easy to implement, because $\tilde{F}$ is not an easily verifiable cash flow (unlike $\tilde{F}I$, which is the cash flow from the investment). Most real-world financial securities, e.g., debt and equity, resemble $\tilde{F}I$ more than they resemble $\tilde{F}$ in that they provide a claim on a cash flow that depends on fundamental and firm action.

Another possible security that features a feedback loop is one that provides a claim on (potentially a proportion of) the net return from the investment $\tilde{F}I - C(I)$. Such a security would have been natural to focus on if $C(I)$ was a monetary cost affecting the firm itself. Technically, however, we are unable to solve a model with this traded security.[17] A key economic difference between $\tilde{F}I$ and $\tilde{F}I - C(I)$ is that the former is always increasing in the level of investment $I$. This is typical to equity of a financially constrained firm, in which shareholders would benefit from having more capital invested in their firm but are constrained in how much capital they can raise due to additional costs that need to be borne by capital providers. Hence, our model is suitable to describe trading of equity of such firms.

Interestingly, this feature is responsible for the fact that in our model we get symmetric frenzies, i.e., both bear raids leading to a decrease in capital and in firm value (as in the recent cases of Bear Stearns and Lehman Brothers) and elevated buying leading to an increase in capital and firm value (as in the Internet or real estate

booms). When speculators buy (sell) they lead the capital provider to invest more (less), which increases (reduces) the value of the security, leading to a profit on their buying (selling). We expect that asymmetric frenzies (i.e., only on the sell side) will exist under the alternative security $\tilde{F}I - C(I)$. This is because, in that case, when speculators sell and reduce the price, they lead the capital provider to provide less capital than optimal and reduce the value of the security, leading to a profit on their selling. But, when they buy and increase the price, they lead the capital provider to provide more capital than optimal and reduce the value of the security, leading to a loss on their buying. However, with the existing techniques, such a model is unsolvable.

## 5. The determinants of speculators' coordination

The weight that speculators put on the common signal in this model is affected by the degree to which there are strategic complementarities or strategic substitutes among them. To see the sources of the two types of strategic interaction, recall from Eq. (3) that a speculator's expected profit is $x(i)E[(1-\beta)\tilde{F}I - P|\mathcal{F}_i]$. When other speculators put more weight on the common signal, this signal gets to have a stronger effect on the price $P$, as well as on the real value of the security $(1-\beta)\tilde{F}I$ (because the capital provider's investment decision is affected by the price). The first effect pushes the speculator to put a lower weight on the common signal, because relying on the common signal more heavily implies paying a high price when buying and getting a low price when selling. The second effect pushes the speculator to put a higher weight on the common signal, because relying on the common signal more heavily implies buying a security with high value and selling one with low value. Hence, the source of strategic substitutes in our model is the price mechanism, which is usual in models of financial markets, while the source of strategic complementarities is the feedback effect to the real value of the security.

In a world without these strategic interactions, the weight that speculators put on the common signal relative to the private signal would be equal to the ratio of precisions between the signals: $\tau_c/\tau_s$. But, with strategic interactions, the equilibrium weight on the common signal $k^*$ reflects the sum of the effects of the strategic interactions on top of the precisions ratio, in which the strategic substitutes due to the price mechanism push $k$ down and the strategic complementarities due to the feedback effect push it up. We formally isolate the various determinants of coordination to understand the impact of each factor on the equilibrium level of coordination.

### 5.1. Impact of learning by the capital provider

Traditionally, financial markets are modeled in the finance literature as a side show. They reflect firms' cash flows but do not affect them. In our model, the financial market has an effect on the firm's investment and cash flow via the learning from the price by the capital provider. Our paper shows that this feedback effect is a source of strategic complementarities that lead to trading frenzies in

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[17] To see this, go back to Eq. (12). The expected value of the security for a speculator $(1-\beta)E[\tilde{F}I|\tilde{s}_i, \tilde{s}_c]$ is expressed there as one exponential term (given our log-normal distributions), which is crucial for our ability to find a linear solution. If the cash flow from the traded security was proportional to $\tilde{F}I - C(I)$, we would have two exponential terms, which would render the steps for finding a linear solution impossible.

the financial market. In this subsection, we demonstrate this formally by comparing our main model with a model with no feedback effect from prices to firms' investments and cash flows because the capital provider does not learn from the price. We show that strategic complementarities emerge only in our main model, leading speculators to put a larger weight on the common signal.

In the absence of feedback from the market, the capital provider's decision on how much capital to provide becomes [this equation is analogous to Eq. (11) in the main model]:

$$I = \frac{\beta}{c} E[\tilde{F}|\tilde{s}_l = s_l] = \frac{\beta}{c} \exp\left( \frac{\tau_f \overline{f} + \tau_l s_l}{\tau_f + \tau_l} + \frac{1}{2(\tau_f + \tau_l)} \right). \quad (15)$$

We again solve for the linear monotone equilibrium in which speculators buy the asset if and only if $\tilde{s}_i + k_{BM}\tilde{s}_c \geq g_{BM}$ (the subscript $BM$ stands for benchmark) and sell the asset otherwise. Given the investment rule in Eq. (15), the expected profit for speculator $i$ from buying the asset, given the information available to him, becomes [this equation is analogous to Eq. (12) in the main model]:

$$E[(1-\beta)\tilde{F}I - P|\tilde{s}_i, \tilde{s}_c]$$
$$= E\left[ \frac{\beta(1-\beta)}{c} \exp\left( \frac{\tau_f \overline{f} + \tau_l s_l}{\tau_f + \tau_l} + \frac{1}{2(\tau_f + \tau_l)} \right) \tilde{F}|\tilde{s}_i, \tilde{s}_c \right]$$
$$- E\left[ \exp\left( \frac{1}{\alpha \sigma_s} (\tilde{f} + k_{BM}\tilde{s}_c - g_{BM} + \sigma_s \tilde{\xi}) \right) \Big| \tilde{s}_i, \tilde{s}_c \right]. \quad (16)$$

For a speculator who buys the asset, Eq. (16) must be positive. Taking expectation and rearranging, we can see that a speculator buys the asset if and only if $\tilde{s}_i + B_{BM}(k)\tilde{s}_c \geq C_{BM}$, where

$$B_{BM}(k) = \frac{\tau_c}{\tau_s} - \frac{\frac{\sqrt{\tau_s}}{\alpha}k}{\frac{\tau_s}{\tau_f + \tau_s + \tau_c}\left( \frac{\tau_f + 2\tau_l}{\tau_f + \tau_l} - \frac{\sqrt{\tau_s}}{\alpha} \right)}. \quad (17)$$

Solving $B_{BM}(k) = k$, as in the main model, we obtain the equilibrium weight that speculators put on the common signal in the case of no feedback effect from price to real investment:

$$k_{BM} = \frac{\left( \left( 1 - \frac{\sqrt{\tau_s}}{\alpha} \right)\tau_f + \left( 2 - \frac{\sqrt{\tau_s}}{\alpha} \right)\tau_l \right)\tau_c}{\left( \frac{\sqrt{\tau_s}}{\alpha} \right)(\tau_f + \tau_l)(\tau_c + \tau_f + \tau_s) + \left( \left( 1 - \frac{\sqrt{\tau_s}}{\alpha} \right)\tau_f + \left( 2 - \frac{\sqrt{\tau_s}}{\alpha} \right)\tau_l \right)\tau_s}.^{18}$$
$$(18)$$

Inspecting Eq. (18), we can see that $k_{BM}$ is lower than $\tau_c/\tau_s$ and that it approaches $\tau_c/\tau_s$ as $\alpha$ gets very large. The intuition is as follows: $\tau_c/\tau_s$ represents the ratio of precisions between the common signal and the idiosyncratic signal. This is the relative weight that speculators would put on the common signal if there were no strategic interactions. In a world without a feedback effect, the only strategic interaction between the speculators comes from the price mechanism, which generates strategic substitutes that reduce $k_{BM}$ below $\tau_c/\tau_s$. As $\alpha$ gets very large, this effect weakens, because the supply is highly elastic in the

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[18] The expression for $C_{BM}$ and other details are in the proof of Proposition 2.

price, and so the price is not strongly affected by speculators' trades. Hence, speculators converge to the weight of $\tau_c/\tau_s$.

Proposition 2 summarizes the properties of $k_{BM}$ and its relation to the equilibrium weight $k^*$ in the main model.

*Proposition 2. If the capital provider does not learn from the price when making lending decisions, the weight speculators put on the common signal $k_{BM}$ is given by Eq. (18). For a high enough level of supply elasticity $\alpha$, $k_{BM}$ is strictly below the equilibrium weight $k^*$ that speculators put on the common signal in the main model (with a feedback effect).*

When we shut down the feedback effect from the price to real investment, the weight that speculators put on the common signal decreases. This is in line with our discussion above, according to which the feedback effect from prices to real investment is the source of complementarity in speculators' strategies, making them want to put more weight on the common signal. Hence, the feedback effect is the cause of trading frenzies in our model.

For illustration, we plot the best response function for our main model [as in Eq. (14)] and for the benchmark case [as in Eq. (17)] in Fig. 1. In the figure, the intersections of $B(k)$ and $B_{BM}(k)$ with the 45° line establish the equilibrium weights $k^*$ and $k_{BM}$, respectively. As seen in the figure, $B(0) = B_{BM}(0) = \tau_c/\tau_s$. That is, in both cases, if other speculators put no weight on the common signal, a speculator finds it optimal to use the ratio of precisions between the common signal and the idiosyncratic signal as the weight for the common signal. This is because when other speculators do not put weight on the common signal, this signal is essentially like a private signal and, hence, it gets weighted solely based on its precision.

Once $k$ increases above zero, strategic substitutability from the price mechanism emerges in the benchmark model. Indeed, the best response $B_{BM}(k)$ is a decreasing
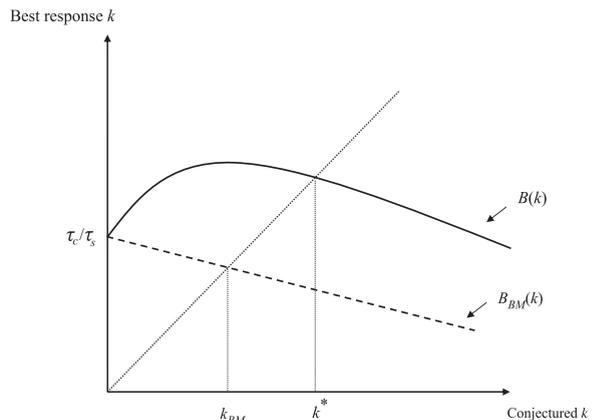


**Fig. 1.** Best response functions. The *x*-axis denotes a given speculator's conjecture about the weight on the common signal by others. The *y*-axis denotes the weight that he puts on the common signal as best response. The best response function in the main model, $B(k)$, is given by the solid line and the best response function in the benchmark model without learning, $B_{BM}(k)$, is given by the dashed line. The intersection of the best response function with the 45° line (the dotted line) yields the equilibrium outcome in the main model $k^*$ and in the benchmark case $k_{BM}$, respectively.

function of $k$. When others put more weight on the common signal, this signal gets more strongly reflected in the price, making an individual speculator reduce the weight he puts on the common signal. By contrast, in our main model, in addition to strategic substitutability from the price mechanism, strategic complementarity emerges due to the feedback effect. For $\alpha$ large enough, the effect from strategic complementarity dominates that from strategic substitutability, resulting in $B(k)$ increasing above $\tau_c/\tau_s$. As the figure shows, this results in a higher equilibrium weight on the common signal in the main model than in the benchmark model, which is proved formally in the proof of Proposition 2.

## 5.2. Impact of supply elasticity

The parameter $\alpha$ captures the elasticity of supply with respect to price in our model. When $\alpha$ is high, the supply of shares is very sensitive to the price, meaning that an increase in demand by informed traders is quickly absorbed in the market, so that informed trading does not have a large price impact. The parameter $\alpha$ can then be interpreted as a measure of liquidity. It can be measured empirically as the inverse of the sensitivity of price to order flow. Amihud (2002) has developed such an empirical proxy based on the sensitivity of daily returns to daily volume. Proposition 3 shows that, in our model, the extent to which speculators coordinate on the common signal increases in the level of liquidity $\alpha$.

**Proposition 3.** *The equilibrium level of coordination $k^*$ is increasing in the supply elasticity $\alpha$, and for $\alpha$ large enough $k^*$ is greater than the precisions ratio $\tau_c/\tau_s$.*

In illiquid markets, order flows have a large effect on the price. Then, when speculators put more weight on the common signal, this signal has a substantial effect on the price, and so other speculators want to put less weight on the common signal. This effect decreases as $\alpha$ goes up and liquidity improves. Hence, in liquid markets there is a greater tendency for coordination and trading frenzies. As the proposition shows, when $\alpha$ is large enough, the weight on the common signal increases beyond the ratio of precisions $\tau_c/\tau_s$.

The positive effect of $\alpha$ on $k$ exists also in the benchmark model described in Section 5.1, in which trading in the financial market has no effect on the firm's cash flows. The feedback effect from trading to the firm's cash flow strengthens this effect, because once speculators start putting more weight on the common signal, the feedback effect to cash flow induces others to increase the weight on the common signal even more. A feature of our model that is crucial for this is that the feedback effect of speculators' trading on the real investment does not weaken when liquidity increases. Even though a high level of liquidity implies that prices change less with order flows, the capital provider is aware of this and, hence, becomes more tuned to small changes in the price, such that the sensitivity of investment to trading activity remains unaffected.

## 5.3. Impact of noise trading

Noise trading is captured in our model by the variable $\tilde{\xi} \sim N(0, \sigma_\xi^2)$. A high level of $\sigma_\xi^2$ implies that the market is exposed to large levels of noise trading. In the literature on financial markets, this introduces noise to the price, and in the presence of a feedback effect, it makes it harder to base investment decisions on the price. In our model, we examine the effect of noise trading on speculators' coordination. This will have further implications for the informativeness of the price.

**Proposition 4.** *For a high enough level of supply elasticity $\alpha$, the equilibrium weight $k^*$ that speculators put on the common signal is decreasing in the variance of noise trading $\sigma_\xi^2$.*

The intuition here goes as follows: With high variance in the noise demand, there is high variance in the market price for reasons that are not related to speculators' trades. As a result, the reliance of the capital provider on the information in the price decreases. This weakens the feedback effect and, hence, the strategic complementarities among speculators, leading to a lower level of $k^*$. Empirically, one can expect different types of traders to be prone to liquidity shocks to a different extent. For example, it is known that mutual funds are subject to large variation in redemptions, whereas hedge funds put tighter restrictions on redemptions and so are less exposed to them. Hence, the effect in our model would lead stocks held by mutual funds to be less exposed to trading frenzies by informed speculators than stocks held by hedge funds.

Changes in the position limits of speculators have similar effects to changes in the variance of noise trading. For example, if speculators could choose positions in the range $[-2, 2]$ (instead of $[-1, 1]$, assumed in the paper), they would have more impact on the capital provider's decision for a given level of $\sigma_\xi^2$ and, thus, would put a larger weight on the common signal in equilibrium. Hence, the effect of loosening speculators' trading constraints is similar to that of reducing the variance of noise trading.

## 5.4. Impact of the information structure

We now establish comparative statics results on the effect of the informativeness of various signals on the equilibrium level of coordination. The results are summarized in Proposition 5.

**Proposition 5.** *For a high enough level of supply elasticity $\alpha$, the equilibrium level of coordination $k^*$ decreases in the precision of speculators' private signals $\tau_s$, increases in the precision of their common signal $\tau_c$, and decreases in the precision of the capital provider's signal $\tau_l$.*

These results are intuitive. Speculators put more weight on the common signal relative to the private signal when the common signal is more precise ($\tau_c$ is higher) and the private signal is less precise ($\tau_s$ is lower). Hence, trading frenzies are more likely when the common information becomes more precise relative to speculators' idiosyncratic sources of information. Less obvious is the result that the

tendency for coordination among speculators decreases when the capital provider has more precise information ($\tau_l$ is higher). The reason is that when the capital provider has more precise information, he relies less on the price, and so the feedback effect from markets to real decisions weakens, and there is less scope for strategic complementarities.

Empirically, we could expect that the market will not have very precise information about the technology used by the firm and will have better information about the demand for the firm's products. This implies that, in relative terms, capital providers, who are closer to the firm than speculators, will have more precise information about firms with technological uncertainties and less precise information about firms with demand uncertainties, and so the latter will be more likely to be subject to a trading frenzy. It is more difficult to get a proxy for the precision of common market information relative to private speculators' information. The recent phenomenon in which speculators exchange information in forums over the Internet could help provide such empirical proxies. A large volume of activity in such forums could suggest that speculators have more common information than private information and so trading frenzies become more likely to occur.

## 6. Coordination, investment efficiency, and nonfundamental volatility

In this section, we explore the effect that coordination has on the efficiency of investment decisions. Vives (1993) and other authors show how the reliance of agents on public information imposes negative externalities on other agents, as it reduces the efficiency of learning. In our paper, the weight that speculators put on common information increases due to strategic complementarities that emerge as a result of the informational feedback from the market to real investment. We explore the implications that this generates for the efficiency of real investment.

To analyze investment efficiency, we look at the ex ante expected net benefit of investment (i.e., expected net benefit before any of the signals are realized given the prior belief that $\tilde{f}$ is normally distributed with mean $\bar{f}$ and precision $\tau_f$). We keep the information structure the same as before and in particular in the interim stage we allow the capital provider to obtain information only from his private signal and the price. So our efficiency criterion is given by

$$E_0\left[\max_I E\left[\tilde{f}I - \frac{1}{2}cI^2 \middle| \tilde{s}_l = s_l, P\right]\right], \tag{19}$$

where a speculator purchases the asset if $\tilde{s}_i + k\tilde{s}_c \geq g$ and shorts it otherwise (for constant $k$ and $g$) and $P$ is the market clearing price. We denote the optimal level of coordination $k_{OP}$ to be the one that maximizes investment efficiency as in Eq. (19).[19]

Proposition 6 characterizes $k_{OP}$ and how it is linked to the accuracy of the information inferred from the market price, $\tau_p$.

*Proposition 6. The level of coordination that maximizes investment efficiency is $k_{OP} = \tau_c/(\tau_s \tau_\xi)$, which also maximizes the precision of the price $\tau_p$.*

The capital provider cares about the events in the security market only to the extent that they affect the quality of the information he has when making the investment decision. Hence, the level of coordination that maximizes investment efficiency is the one that maximizes the accuracy of the information in the market price. This is a result of the fact that the financial market in our model affects the investment decision only via the information provided by the market to the capital provider. This is a broad insight that extends beyond the model and should hold in other settings. When the financial market is a secondary market, its effect on the real decisions comes only from the information it provides, and so real efficiency is determined by the precision of the information that the market provides about the variable that decision makers care to learn (in our model, this is $\tilde{f}$).

Examining the expression for the price signal in Eq. (9), we can see that a trade-off exists in setting the level of coordination. The trade-off arises because there are two sources of noise in the price, one coming from the noise trading $\tilde{\xi}$ and the other one from the noise in the common signal $\tilde{\epsilon}_c$. (The first source of noise becomes more prominent when speculators' private information is noisy—$\tau_s$ is low—then noise trading becomes relatively more important.) A high level of coordination reduces the effect of the first source of noise (as coordinated speculative trading helps overcome the large volume of noise trading) and increases the effect of the second source of noise (as coordinated speculative trading increases the weight on the common signal). Therefore, the optimal level of coordination is high when the potential damage from noise trading is high ($\tau_\xi$ and $\tau_s$ are low) or when the potential damage from noise in the common signal is low ($\tau_c$ is high). Then, $k_{OP} = \tau_c/(\tau_s \tau_\xi)$.

It is interesting to compare the optimal level of coordination characterized here with the level of coordination that is obtained in equilibrium. From Proposition 4, in equilibrium speculators coordinate more when the variance in the noise trading is low ($\tau_\xi$ is high). A high $\tau_\xi$ implies that speculators' trades have more effect on the capital provider's decision, increasing the scope of strategic complementarities. Yet, this is exactly when coordination is not desirable for the efficiency of the investment. Hence, a sharp contrast exists between the profit incentives of speculators and between price informativeness and investment efficiency. Speculators coordinate more exactly when it is inefficient to do so. Proposition 7 summarizes the comparison between the optimal level of coordination and the equilibrium level of coordination.

*Proposition 7. For a high enough level of supply elasticity $\alpha$, there exists $\overline{\tau}_\xi$ such that the level of coordination that maximizes investment efficiency is greater than the equilibrium level of coordination ($k_{OP} > k^*$) when the precision of*

---

[19] We focus only on the efficiency of real investment and so ignore other implications that trading could have on welfare via the transfer of resources across traders in the financial market. Accounting for these other effects would require a model with endogenous noise trading.

the noise trading distribution $\tau_\xi$ is below $\overline{\tau}_\xi$. Similarly, $k_{OP} < k^*$ for $\tau_\xi > \overline{\tau}_\xi$.

The proposition says that speculators coordinate too much in markets with less noise trading and coordinate too little in markets with more noise trading. Interestingly, this implies that trading frenzies are only sometimes undesirable. When there is high variation in noise trading, price informativeness would improve if speculators coordinated their trades more to provide a signal that overcomes the effect of noise trading. Yet, it is exactly in this case that they find coordination less profitable in equilibrium.

Proposition 8 considers the positive implications of inefficient coordination levels. Deviations from the optimal level of coordination $k_{OP}$ are manifested in our model by higher levels of nonfundamental volatility. We define this as volatility that does not come from the variability in fundamental.

*Proposition 8. Nonfundamental volatility of asset price is minimized at $k = k_{OP}$ [where its value is $1/(\tau_c + \tau_s\tau_\xi)$]. Similarly, nonfundamental volatility of investment is minimized at $k = k_{OP}$ [where its value is $1/(\tau_l + \tau_c + \tau_s\tau_\xi)$].*

This proposition indicates that the strategic interactions among speculators in the financial markets often lead to nonfundamental volatility in prices as well as real activities. The source of this nonfundamental volatility could come from either too low coordination (that is, when the market is characterized by a high amount of noise trading) or too high coordination (that is, when the market has low noise trading and the noise in the correlated signals among speculators is high). Nonfundamental volatility is difficult to measure because it is defined as the volatility that does not come from fundamentals, while the volatility of fundamentals is unobservable (the volatility of cash flow is observable but includes volatility due to noise). Hence, this notion is interesting mostly for theoretical reasons.

Finally, the analysis in this section can provide a basis for policy discussions regarding the role of financial markets in the economy and potential ways to regulate them. Regulatory agencies, such as the SEC, are often concerned about the damaging effect of speculative trading, and calls are often made for intervention in speculative markets. However, it is hard to justify such interventions in models in which the financial market is a side show and does not have a feedback effect on the real economy. As we show in this section, trading patterns in the financial market have an effect on the efficiency of real investment, and so this could provide a reason for intervention in financial market trading.

It is tempting to suggest that changing the level of noise trading (by changing $\tau_\xi$) or, equivalently, changing the level of informed trading (by changing the position limits of speculators) is a tool that the government can use to influence the strength of trading frenzies and, hence, also the level of real investment efficiency. After all, Proposition 4 shows that trading frenzies are stronger (i.e., $k^*$ is larger) when $\tau_\xi$ is higher (or when speculators can trade more aggressively). Combining this result with

Proposition 7, one might think that decreasing $\tau_\xi$ (or decreasing the size of speculators' positions) can improve efficiency when $\tau_\xi > \overline{\tau}_\xi$ and, similarly, that increasing $\tau_\xi$ (or increasing the size of speculators' positions) can improve efficiency when $\tau_\xi < \overline{\tau}_\xi$. However, $\tau_\xi$ and the size of speculators' positions also have a direct effect on investment efficiency, which goes beyond their effect via $k^*$. The direct effect always calls for increasing $\tau_\xi$ and the size of speculators' positions, as this means that there is more information in prices. In numerical analysis, it appears that the direct effect always dominates the indirect effect via $k^*$. Hence, while regulators are sometimes tempted to limit speculative positions, our model suggests that this might not be wise, as the reduction of informed trading that comes as a direct result of this is damaging to price informativeness and investment efficiency, and this is stronger than the potential benefit from weakening the trading frenzy.

One parameter that can provide a useful policy tool in our framework is the liquidity level $\alpha$. This is because $\alpha$ has no direct effect on the informativeness of the price and the efficiency of investment. It affects them only via its effect on the trading frenzy $k^*$. Hence, combining the results from Propositions 3 and 7, our model suggests that it is beneficial for the government to try to increase $\alpha$ (and so increase $k^*$) when $\tau_\xi$ is below $\overline{\tau}_\xi$. Similarly, it is beneficial for the government to try to decrease $\alpha$ (and so decrease $k^*$) when $\tau_\xi$ is above $\overline{\tau}_\xi$. The parameter $\alpha$ represents the sensitivity of order flows to prices, and so increasing $\alpha$ would amount to buying more when the price decreases and selling more when the price increases. Changing $\alpha$ can be accomplished by having the government trade in the market in response to prices or allowing more brokers or market makers to operate in the market and provide such liquidity.

## 7. Conclusion

We study strategic interactions among speculators in financial markets and their real effects. Two opposite strategic interactions exist. On the one hand, speculators wish to act differently from each other as a certain action by other speculators changes the price in a way that reduces the profit for other speculators from this action. On the other hand, due to the feedback effect from the price to the real investment, a certain action by speculators changes the real value of the firm in a way that increases the incentive of other speculators to take this action. This creates a basis for trading frenzies, in which speculators rush to trade in the same direction, putting pressure on the price and on the firm's value. We characterize which effect dominates when and analyze the resulting level of coordination in speculators' actions.

The interaction among speculators affects the informational content of the price. Because prices affect real investment in our model, we can ask what level of coordination is most efficient for real investment. In general, speculators' incentives to coordinate go in the opposite direction of the optimal level of coordination.

Speculators want to coordinate more when there is a low amount of noise trading, but this is when coordination is less desirable from an efficiency point of view. Hence, our model shows that there is always either too much or too little coordination, and this reduces the efficiency of investment and creates excess volatility in the price.

Interestingly, our paper is also related to an old debate on whether speculators stabilize prices. The traditional view is that by buying low and selling dear, rational speculators stabilize prices. Hart and Kreps (1986) argue that when speculators can hold inventories and there is uncertainty about preferences, speculative activity could cause excess price movement. Our paper contributes to this literature by pointing out that when speculative activity has an effect on real investments, speculators might coordinate on correlated sources of information. This affects the excess volatility in prices and the efficiency of real investments.

# Appendix A

## A.1. Proof of Proposition 1

Based on Eq. (12) and the updating done by the speculator based on his information, the coefficients in (13) are given as

$$
a_0 = \frac{\tau_f \overline{f} + \frac{1}{2}}{\tau_f + \tau_l + \tau_p} + \frac{\left(\tau_f + 2\tau_l + \tau_p\left(1 + \frac{1}{1+k}\right)\right)}{\tau_f + \tau_l + \tau_p}
$$

$$
\left(\frac{\tau_f \overline{f}}{\tau_f + \tau_s + \tau_c}\right) + \left(\frac{\tau_f + 2\tau_l + \left(1 + \frac{1}{1+k}\right)\tau_p}{\tau_f + \tau_l + \tau_p}\right)^2
$$

$$
\frac{1}{2(\tau_f + \tau_s + \tau_c)} + \frac{1}{2}\left(\frac{\tau_l}{\tau_f + \tau_l + \tau_p}\right)^2 \sigma_l^2
$$

$$
+ \frac{1}{2}\left(\frac{\tau_p}{\tau_f + \tau_l + \tau_p}\right)^2 \left(\frac{1}{1+k}\right)^2 \sigma_s^2 \sigma_\xi^2, \tag{20}
$$

$$
a_1 = \frac{\left(\tau_f + 2\tau_l + \tau_p\left(1 + \frac{1}{1+k}\right)\right)}{\tau_f + \tau_l + \tau_p} \frac{\tau_s}{\tau_f + \tau_s + \tau_c}, \tag{21}
$$

$$
a_2 = \frac{\tau_p \frac{k}{1+k}}{\tau_f + \tau_l + \tau_p}
$$

$$
+ \frac{\left(\tau_f + 2\tau_l + \tau_p\left(1 + \frac{1}{1+k}\right)\right)}{\tau_f + \tau_l + \tau_p} \frac{\tau_c}{\tau_f + \tau_s + \tau_c}, \tag{22}
$$

$$
b_0 = \frac{1}{\alpha\sigma_s}\left(\frac{\tau_f \overline{f} + \frac{1}{2}\frac{1}{\alpha\sigma_s}}{\tau_f + \tau_s + \tau_c} - g\right) + \frac{1}{2\alpha^2}\sigma_\xi^2, \tag{23}
$$

$$
b_1 = \frac{1}{\alpha\sigma_s}\frac{\tau_s}{\tau_f + \tau_s + \tau_c}, \tag{24}
$$

and

$$
b_2 = \frac{1}{\alpha\sigma_s}\left(\frac{\tau_c}{\tau_f + \tau_s + \tau_c} + k\right). \tag{25}
$$

Note that

$$
a_1 - b_1 = \frac{\tau_s}{\tau_f + \tau_s + \tau_c}\left(\frac{\left(\tau_f + 2\tau_l + \tau_p\left(1 + \frac{1}{1+k}\right)\right)}{\tau_f + \tau_l + \tau_p} - \frac{1}{\alpha\sigma_s}\right). \tag{26}
$$

A sufficient condition for $a_1 - b_1 > 0$ is that $\alpha > \sqrt{\tau_s}$. Recall that $B(k) = (a_2 - b_2)/(a_1 - b_1)$. Substituting, we obtain

$$
B(k) = \frac{\frac{\tau_p \frac{k}{1+k}}{\tau_f + \tau_l + \tau_p} + \frac{\left(\tau_f + 2\tau_l + \tau_p\left(1 + \frac{1}{1+k}\right)\right)}{\tau_f + \tau_l + \tau_p}\frac{\tau_c}{\tau_f + \tau_s + \tau_c} - \frac{1}{\alpha\sigma_s}\left(\frac{\tau_c}{\tau_f + \tau_s + \tau_c} + k\right)}{\frac{\tau_s}{\tau_f + \tau_s + \tau_c}\left(\frac{\left(\tau_f + 2\tau_l + \tau_p\left(1 + \frac{1}{1+k}\right)\right)}{\tau_f + \tau_l + \tau_p} - \frac{1}{\alpha\sigma_s}\right)}. \tag{27}
$$

Simplifying $B(k) - k = 0$, we get

$$
0 = \left[\frac{1}{\tau_s}\frac{(k+1)(\tau_c + \tau_f + \tau_s)(\tau_f + \tau_l + \tau_p)}{\tau_p + (k+1)\tau_l + \left(1 - \frac{\sqrt{\tau_s}}{\alpha}\right)(1+k)(\tau_f + \tau_l + \tau_p)}\right]
$$

$$
\left(\frac{\tau_p}{\tau_f + \tau_l + \tau_p}\frac{k}{1+k} + \frac{\left(\tau_f + 2\tau_l + \left(1 + \frac{1}{1+k}\right)\tau_p\right)}{\tau_f + \tau_l + \tau_p}\right)
$$

$$
\left(\frac{-\tau_s k + \tau_c}{\tau_f + \tau_s + \tau_c}\right) - \frac{\sqrt{\tau_s}}{\alpha}\left(\left(\frac{-\tau_s k + \tau_c}{\tau_f + \tau_s + \tau_c}\right) + k\right)\right). \tag{28}
$$

The term in square brackets is strictly positive for $\alpha > \sqrt{\tau_s}$. So the equilibrium condition can be simplified to

$$
0 = \frac{\tau_p}{\tau_f + \tau_l + \tau_p}\frac{k}{1+k} + \frac{\left(\tau_f + 2\tau_l + \left(1 + \frac{1}{1+k}\right)\tau_p\right)}{\tau_f + \tau_l + \tau_p}
$$

$$
\left(\frac{-\tau_s k + \tau_c}{\tau_f + \tau_s + \tau_c}\right) - \left(\frac{-\tau_s k + \tau_c}{\tau_f + \tau_s + \tau_c}\right) - k
$$

$$
+ \left(1 - \frac{1}{\alpha\sigma_s}\right)\left(\frac{\tau_f + \tau_c}{\tau_f + \tau_s + \tau_c}k + \frac{\tau_c}{\tau_f + \tau_s + \tau_c}\right). \tag{29}
$$

Recall that $\tau_p = ((1+k)^2 \tau_c \tau_\xi \tau_s)/(k^2 \tau_\xi \tau_s + \tau_c)$. We denote $r \equiv \tau_\xi \tau_s$. Substituting for $\tau_p$ and simplifying, the right-hand side becomes

$$
H(k) = -k^3((\tau_c + \tau_f + \tau_s)(\tau_c + \tau_f + \tau_l) + \tau_l \tau_s)
$$

$$
- \tau_c k^2(\tau_c + \tau_f - \tau_l + 2\tau_s) - \tau_c k(\tau_s - \tau_c) + \tau_c^2
$$

$$
- \frac{1}{r}(\tau_c k(\tau_c \tau_f + \tau_c \tau_l + \tau_f \tau_l + \tau_f \tau_s + 2\tau_l \tau_s + \tau_f^2) - \tau_c^2 \tau_l)
$$

$$
+ \left(1 - \frac{\sqrt{\tau_s}}{\alpha}\right)((\tau_c + \tau_f)(\tau_c + \tau_f + \tau_l)k^3
$$

$$
+ \tau_c(3\tau_c + 3\tau_f + \tau_l)k^2 + \tau_c(\tau_f + 3\tau_c)k + \tau_c^2)
$$

$$
+ \left(1 - \frac{\sqrt{\tau_s}}{\alpha}\right)\frac{\tau_c}{r}((\tau_f + \tau_l)(\tau_c + \tau_f)k + \tau_c(\tau_f + \tau_l)).^{[20]} \tag{30}
$$

For an equilibrium, we need $H(k) = 0$.

---

[20] The simplification is achieved by dividing by $r$ and multiplying through with $(\tau_c + \tau_f + \tau_s)(\tau_c \tau_f + \tau_c \tau_l + \tau_c r + \tau_c k^2 r + \tau_f k^2 r + k^2 \tau_l r + 2\tau_c k r)$.

First, we focus on existence of an equilibrium with $k > 0$. $H(k)$ has a positive root if and only if

$$\alpha > \sqrt{\tau_s} \frac{\tau_f + \tau_l + r}{\tau_f + 2\tau_l + 2r}. \tag{31}$$

To see this, note that the coefficient for $k^3$ is always negative, implying that the value of $H(k)$ becomes negative as $k$ becomes large. So, there exists a strictly positive root for the polynomial if its value at $k=0$ is strictly positive. This condition is given by the above inequality. If the inequality is violated, the value of the polynomial is negative at $k=0$. Its derivative at $k=0$ is given by

$$-\tau_c(\tau_s - \tau_c) - \frac{1}{r}(\tau_c(\tau_c\tau_f + \tau_c\tau_l + \tau_f\tau_l + \tau_f\tau_s + 2\tau_l\tau_s + \tau_f^2))$$
$$+ \left(1 - \frac{\sqrt{\tau_s}}{\alpha}\right)\tau_c(\tau_f + 3\tau_c) + \left(1 - \frac{\sqrt{\tau_s}}{\alpha}\right)\frac{\tau_c}{r}((\tau_f + \tau_l)(\tau_c + \tau_f)). \tag{32}$$

At $(\sqrt{\tau_s}/\alpha) \geq (\tau_f + 2\tau_l + 2r)/(\tau_f + \tau_l + r)$ the derivative is negative. This means that $H(k)$ is decreasing at $k=0$ for $(\sqrt{\tau_s}/\alpha) \geq (\tau_f + 2\tau_l + 2r)/(\tau_f + \tau_l + r)$. Moreover, the second derivative is negative when $(\sqrt{\tau_s}/\alpha) \geq (\tau_f + 2\tau_l + 2r)/(\tau_f + \tau_l + r)$ and, thus, the expression keeps decreasing. Therefore, the polynomial cannot have a positive root.

For uniqueness, we need to check the sign of the discriminant of $H(k)$ for $\alpha$ large and $\tau_f$ small. Letting $\alpha$ go to infinity and $\tau_f$ go to zero, we obtain the discriminant as $-\tau_c^3/r^3$ times

strictly negative for large enough $\alpha$ and small enough $\tau_f$ and, hence, $H(k) = 0$ has a unique root. □

### A.2. Proof of Propositions 2

First, we derive $k_{BM}$. Based on Eq. (16) and taking expectations, we see that a speculator buys the asset when

$$\ln\left(\frac{\beta(1-\beta)}{c}\right) + \frac{\tau_f \overline{f} + \frac{1}{2}}{\tau_f + \tau_l} + \left(\frac{\tau_f + 2\tau_l}{\tau_f + \tau_l}\right)\left(\frac{\tau_f \overline{f} + \tau_s \tilde{s}_i + \tau_c \tilde{s}_c}{\tau_f + \tau_s + \tau_c}\right)$$
$$+ \left(\frac{\tau_f + 2\tau_l}{\tau_f + \tau_l}\right)^2 \frac{1}{2(\tau_f + \tau_s + \tau_c)} + \frac{1}{2}\left(\frac{\tau_l}{\tau_f + \tau_l}\right)^2 \sigma_l^2$$
$$\geq \frac{1}{\alpha \sigma_s}\left(\frac{\tau_f \overline{f} + \tau_s \tilde{s}_i + \tau_c \tilde{s}_c + \frac{1}{2}\frac{1}{\alpha \sigma_s}}{\tau_f + \tau_s + \tau_c} + k_{BM}\tilde{s}_c - g_{BM}\right) + \frac{1}{2\alpha^2}\sigma_\xi^2. \tag{36}$$

Rearranging Eq. (36), a speculator buys the asset when $\tilde{s}_i + B_{BM}(k_{BM})\tilde{s}_c \geq C_{BM}$, where

$$B_{BM}(k_{BM}) = \frac{\tau_c}{\tau_s} - \frac{\frac{\sqrt{\tau_s}}{\alpha}k_{BM}}{\frac{\tau_s}{\tau_f + \tau_s + \tau_c}\left(\frac{\tau_f + 2\tau_l}{\tau_f + \tau_l} - \frac{\sqrt{\tau_s}}{\alpha}\right)} \tag{37}$$

and

$$\left(\begin{array}{c} 64\tau_c^4\tau_l + 128\tau_c^3\tau_l^2 + 160\tau_c^3\tau_l\tau_s + 64\tau_c^2\tau_l^3 + 416\tau_c^2\tau_l^2\tau_s + 144\tau_c^2\tau_l\tau_s^2 \\ + 284\tau_c\tau_l^2\tau_s^2 + 56\tau_c\tau_l\tau_s^3 + 8\tau_l\tau_s^4 \end{array}\right)r^3$$
$$+ \left(\begin{array}{c} 64\tau_c^5\tau_l + 192\tau_c^4\tau_l^2 + 160\tau_c^4\tau_l\tau_s + 192\tau_c^2\tau_l^3 + 608\tau_c^3\tau_l^2\tau_s + 144\tau_c^3\tau_l\tau_s^2 + 64\tau_c^2\tau_l^4 \\ + 448\tau_c^2\tau_l^3\tau_s + 440\tau_c^2\tau_l^2\tau_s^2 + 56\tau_c^2\tau_l\tau_s^3 + 416\tau_c\tau_l^3\tau_s^2 + 80\tau_c\tau_l^2\tau_s^3 + 8\tau_c\tau_l\tau_s^4 + 48\tau_l^2\tau_s^4 \end{array}\right)r^2$$
$$+ (128\tau_c\tau_l^4\tau_s^2 - 32\tau_c^2\tau_l^3\tau_s^2 - 16\tau_c^2\tau_l^2\tau_s^3 - 52\tau_c^3\tau_l^2\tau_s^2 - 64\tau_c\tau_l^3\tau_s^3 + 32\tau_c\tau_l^2\tau_s^4 + 96\tau_l^3\tau_s^4)r + (64\tau_l^4\tau_s^4 + 32\tau_c\tau_l^3\tau_s^4). \tag{33}$$

The coefficient of $r^2$ in Eq. (33) is strictly positive so the quadratic part of Eq. (33) is minimized at

$$r = -\frac{128\tau_c\tau_l^4\tau_s^2 - 32\tau_c^2\tau_l^3\tau_s^2 - 16\tau_c^2\tau_l^2\tau_s^3 - 52\tau_c^3\tau_l^2\tau_s^2 - 64\tau_c\tau_l^3\tau_s^3 + 32\tau_c\tau_l^2\tau_s^4 + 96\tau_l^3\tau_s^4}{2\left(\begin{array}{c} 64\tau_c^5\tau_l + 192\tau_c^4\tau_l^2 + 160\tau_c^4\tau_l\tau_s + 192\tau_c^2\tau_l^3 + 608\tau_c^3\tau_l^2\tau_s + 144\tau_c^3\tau_l\tau_s^2 + 64\tau_c^2\tau_l^4 \\ + 448\tau_c^2\tau_l^3\tau_s + 440\tau_c^2\tau_l^2\tau_s^2 + 56\tau_c^2\tau_l\tau_s^3 + 416\tau_c\tau_l^3\tau_s^2 + 80\tau_c\tau_l^2\tau_s^3 + 8\tau_c\tau_l\tau_s^4 + 48\tau_l^2\tau_s^4 \end{array}\right)}. \tag{34}$$

Substituting this back to the quadratic above, we find that the minimized value is

$$\frac{1}{2}\frac{\tau_l^3\tau_s^4}{\left(\begin{array}{c} 8\tau_c^5 + 24\tau_c^4\tau_l + 20\tau_c^4\tau_s + 24\tau_c^3\tau_l^2 + 76\tau_c^3\tau_l\tau_s + 18\tau_c^3\tau_s^2 + 8\tau_c^2\tau_l^3 + 56\tau_c^2\tau_l^2\tau_s \\ + 55\tau_c^2\tau_l\tau_s^2 + 7\tau_c^2\tau_s^3 + 52\tau_c\tau_l^2\tau_s^2 + 10\tau_c\tau_l\tau_s^3 + \tau_c\tau_s^4 + 6\tau_l\tau_s^4 \end{array}\right)}$$
$$\times \left(\begin{array}{c} 343\tau_c^6 + 2352\tau_c^5\tau_l + 1176\tau_c^5\tau_s + 5376\tau_c^4\tau_l^2 + 6944\tau_c^4\tau_l\tau_s + 1344\tau_c^4\tau_s^2 + 4096\tau_c^3\tau_l^3 \\ + 13,312\tau_c^3\tau_l^2\tau_s + 6448\tau_c^3\tau_l\tau_s^2 + 512\tau_c^3\tau_s^3 + 8192\tau_c^2\tau_l^3\tau_s + 9984\tau_c^2\tau_l^2\tau_s^2 + 1984\tau_c^2\tau_l\tau_s^3 \\ + 5120\tau_c\tau_l^3\tau_s^2 + 2048\tau_c\tau_l^2\tau_s^3 + 128\tau_c\tau_l\tau_s^4 + 192\tau_l^2\tau_s^4 \end{array}\right) \tag{35}$$

which is strictly positive. Because the quadratic term is strictly positive at its minimum, it is positive for all $r$. Because $r^3$ term is positive for $r > 0$ as well, Eq. (33) is strictly positive for all $r > 0$. That is, the discriminant is

$$C_{BM} = \frac{1}{\left(\frac{\tau_f + 2\tau_l}{\tau_f + \tau_l} - \frac{1}{\alpha \sigma_s}\right)\left(\frac{\tau_s}{\tau_f + \tau_s + \tau_c}\right)}$$

$$\left( \ln(c/\beta(1-\beta)) + \frac{1}{\alpha\sigma_s}\left(\frac{\tau_f\overline{f} + \frac{1}{2}\frac{1}{\alpha\sigma_s}}{\tau_f + \tau_s + \tau_c} - g_{BM}\right) \right)$$
$$- \frac{\tau_f\overline{f} + \frac{1}{2}}{\tau_f + \tau_l} - \left(\frac{\tau_f + 2\tau_l}{\tau_f + \tau_l}\right)\left(\frac{\tau_f\overline{f}}{\tau_f + \tau_s + \tau_c}\right)$$
$$- \left(\frac{\tau_f + 2\tau_l}{\tau_f + \tau_l}\right)^2 \frac{1}{2(\tau_f + \tau_s + \tau_c)} + \frac{1}{2\alpha^2}\sigma_\xi^2 - \frac{1}{2}\left(\frac{\tau_l}{\tau_f + \tau_l}\right)^2 \sigma_l^2. \tag{38}$$

Setting $B_{BM}(k_{BM}) = k_{BM}$ leads to the expression for $k_{BM}$ in Eq. (18).

Now, we show that in the main model (with feedback effect) $k^* > \tau_c/\tau_s$ for $\alpha$ large enough. To see this, note that $H(\tau_c/\tau_s) > 0$ for $\alpha$ large enough. Because $H(k)$ has a unique root and crosses the axis from above, the conclusion follows. Next, note that $k_{BM} < \tau_c/\tau_s$ and thus $k_{BM} < k^*$ for $\alpha$ large enough. □

### A.3. Proof of Proposition 3

We show in the proof of Proposition 2 that $k^* > \tau_c/\tau_s$ for $\alpha$ large enough. By inspecting Eq. (30), we can see that $H(k)$ shifts up as $\alpha$ increases, so its unique root $k^*$ increases in $\alpha$.

### A.4. Proof of Proposition 4

Consider the following terms involving $1/r$ in $H(k)$ in Eq. (30):

$$- \frac{1}{r}(\tau_c k(\tau_c\tau_f + \tau_c\tau_l + \tau_f\tau_l + \tau_f\tau_s + 2\tau_l\tau_s + \tau_f^2) - \tau_c^2\tau_l)$$
$$+ \left(1 - \frac{\sqrt{\tau_s}}{\alpha}\right)\frac{\tau_c}{r}((\tau_f + \tau_l)(\tau_c + \tau_f)k + \tau_c(\tau_f + \tau_l)). \tag{39}$$

For $\alpha$ large enough, these terms are negative if and only if $k$ exceeds $\tau_c/\tau_s$. So for $k > \tau_c/\tau_s$, $H(k)$ shifts up as $r$ goes up. By Proposition 3, for $\alpha$ large enough, $k^*$ that implicitly depends on $r$ exceeds $\tau_c/\tau_s$ for all $r$. because $H(k)$ crosses the axis once from above at $k^*$, we see that $k^*$ must be increasing in $r$. because $\sigma_\xi$ and $r$ are inversely related, an increase in $\sigma_\xi$ leads to a decrease in $k^*$. □

### A.5. Proof of Proposition 5

Let

$$D(k) = -3((\tau_f + \tau_c + \tau_l)(\tau_f + \tau_c + \tau_s) + \tau_l\tau_s)k^2 - 2\tau_c(\tau_f + \tau_c - \tau_l + 2\tau_s)k$$
$$+ \tau_c(\tau_c - \tau_s) - \frac{1}{r}(\tau_c(\tau_f\tau_c + \tau_f\tau_l + \tau_f\tau_s + \tau_c\tau_l + 2\tau_l\tau_s + \tau_f^2))$$
$$+ \left(1 - \frac{\sqrt{\tau_s}}{\alpha}\right)(3(\tau_f + \tau_c)(\tau_f + \tau_c + \tau_l)k^2$$
$$+ 2\tau_c(3\tau_f + 3\tau_c + \tau_l)k + \tau_c(\tau_f + 3\tau_c))$$
$$+ \frac{\tau_c}{r}\left(1 - \frac{\sqrt{\tau_s}}{\alpha}\right)(\tau_f + \tau_c)(\tau_f + \tau_l) \tag{40}$$

Note that $\partial H/\partial k = D(k). = .$ When the equilibrium is unique, $D(k^*) < 0$ because $H(k)$ crosses zero from above.

To see that for $\alpha$ large $\partial k^*/\partial \tau_s < 0$, note for $\alpha$ large, that $\partial k^*/\partial \tau_s$ is arbitrarily close to

$$\frac{\frac{1}{\tau_s^2\tau_\xi}(\tau_c^2\tau_f + 2\tau_c^2\tau_l + \tau_c\tau_s^2\tau_\xi k^* + 2\tau_c\tau_s^2\tau_\xi(k^*)^2 + (\tau_c\tau_s^2\tau_\xi + \tau_f\tau_s^2\tau_\xi + 2\tau_l\tau_s^2\tau_\xi)(k^*)^3)}{D(k^*)} < 0. \tag{41}$$

To see that for $\alpha$ large $\partial k^*/\partial \tau_c > 0$, note for $\alpha$ large, that $\partial k^*/\partial \tau_c$ is arbitrarily close to

$$\frac{\left( \begin{array}{c} \tau_s(k^*)^3 - 2(2\tau_c + \tau_f + \tau_l - \tau_s)(k^*)^2 - (8\tau_c + \tau_f - \tau_s)k^* - 4\tau_c \\ - \frac{1}{r}(-\tau_s(\tau_f + 2\tau_l)k^* + 2\tau_c\tau_f + 4\tau_c\tau_l) \end{array} \right)}{D(k^*)}. \tag{42}$$

Also,

$$\tau_c\left( -\tau_s(k^*)^3 + 2(2\tau_c + \tau_f + \tau_l - \tau_s)(k^*)^2 + (8\tau_c + \tau_f - \tau_s)k^* + 4\tau_c \right.$$
$$+ \frac{1}{r}(-\tau_s(\tau_f + 2\tau_l)k^* + 2\tau_c\tau_f + 4\tau_c\tau_l) \left.\right) > -\tau_s(\tau_c + \tau_f + 2\tau_l)(k^*)^3$$
$$+ 2\tau_c(\tau_f + \tau_l - \tau_s + \tau_c)(k^*)^2 + \tau_c(\tau_f - \tau_s + 4\tau_c)k^* + 2\tau_c^2$$
$$+ \frac{\tau_c}{r}(\tau_c\tau_f + 2\tau_c\tau_l - \tau_s(\tau_f + 2\tau_l)k^*) \tag{43}$$

and the right side of the above inequality is arbitrarily close to $H(k^*)$, which is equal to zero.

Finally, to see that for $\alpha$ large $\partial k^*/\partial \tau_l < 0$, note for $\alpha$ large, that $\partial k^*/\partial \tau_l$ is arbitrarily close to

$$\frac{\frac{2}{r}(k^*\tau_s - \tau_c)(r(k^*)^2 + \tau_c)}{D(k^*)} < 0 \tag{44}$$

because $k^* > \tau_c/\tau_s$. □

### A.6. Proof of Proposition 6

We substitute $I$ from Eq. (2) into Eq. (19) and compute the expectations:

$$\frac{\beta}{c}E\left[\exp(\tilde{f})\exp\left(\frac{\tau_f\overline{f} + \tau_l s_l + \tau_p z(P)}{\tau_f + \tau_l + \tau_p} + \frac{1}{2(\tau_f + \tau_l + \tau_p)}\right)\right]$$
$$- \frac{1}{2}\frac{\beta^2}{c}E\left[\exp\left(2\left(\frac{\tau_f\overline{f} + \tau_l s_l + \tau_p z(P)}{\tau_f + \tau_l + \tau_p} + \frac{1}{2(\tau_f + \tau_l + \tau_p)}\right)\right)\right]$$
$$= \frac{\beta}{c}E\left[\exp\left(2\tilde{f} + \frac{\tau_f(\overline{f} - \tilde{f}) + \tau_l\sigma_l\tilde{e}_l + \tau_p(z(P) - \tilde{f})}{\tau_f + \tau_l + \tau_p}\right.\right.$$
$$+ \left.\left.\frac{1}{2(\tau_f + \tau_l + \tau_p)}\right)\right]$$
$$- \frac{1}{2}\frac{\beta^2}{c}E\left[\exp\left(2\left(\tilde{f} + \frac{\tau_f(\overline{f} - \tilde{f}) + \tau_l\sigma_l\tilde{e}_l + \tau_p(z(P) - \tilde{f})}{\tau_f + \tau_l + \tau_p}\right.\right.\right.$$
$$+ \left.\left.\left.\frac{1}{2(\tau_f + \tau_l + \tau_p)}\right)\right)\right]$$
$$= \frac{\beta}{c}\left(1 - \frac{1}{2}\beta\right)\exp\left(2\overline{f} + \frac{1}{\tau_f}\frac{\tau_f + 2\tau_l + 2\tau_p}{\tau_f + \tau_l + \tau_p}\right). \tag{45}$$

Therefore, the maximization problem can be viewed as maximizing the following expression in $k$:

$$\exp\left(\frac{\tau_f + 2\tau_l + 2\tau_p}{\tau_f + \tau_l + \tau_p}\right), \tag{46}$$

and this is equivalent to maximizing $\tau_p$, which is maximized at $\tau_c/(\tau_s\tau_\xi)$. □

## A.7. Proof of Proposition 7

For $\alpha$ large enough, $H(k)$ evaluated at $k_{OP} = \tau_c/r$ is approximately

$$\frac{\tau_c^2}{r^3}(\tau_c + r)(2\tau_c r - \tau_c \tau_s + 2\tau_f r - \tau_f \tau_s + 2\tau_l r - 2\tau_l \tau_s - r\tau_s + 2r^2), \tag{47}$$

which is negative for $r$ small. Moreover, it could be decreasing in $r$ for $r$ small but eventually increases and becomes positive. This means that a cutoff $\bar{r}$ exists for $r$ such that for $r < \bar{r}$ we have $k^* < k_{OP}$ and for $r > \bar{r}$ we have $k^* > k_{OP}$.  □

## A.8. Proof of Proposition 8

The market clearing price is

$$P = \exp\left(\frac{(1+k)\tilde{f} + k\sigma_c\tilde{\epsilon}_c - g + \sigma_s\tilde{\xi}}{\alpha\sigma_s}\right), \tag{48}$$

and its nonfundamental volatility can be written as the volatility of

$$z(P) - \tilde{f} = \frac{g + \alpha\sigma_s \ln(P)}{1+k} - \tilde{f} = \frac{k}{1+k}\sigma_c\tilde{\epsilon}_c + \frac{\sigma_s}{1+k}\tilde{\xi}. \tag{49}$$

It is straightforward to show that when $k = k_{OP} = \tau_c/(\tau_s\tau_\xi)$, its nonfundamental volatility is the lowest and is

$$\text{Nonfundamental volatility(asset price)} = \frac{1}{\tau_c + \tau_s\tau_\xi}. \tag{50}$$

We know that

$$I = \frac{\beta}{c}\exp\left(\frac{\tau_f\bar{f} + \tau_l s_l + \tau_p\left(\tilde{f} + \frac{k}{1+k}\sigma_c\tilde{\epsilon}_c + \frac{\sigma_s}{1+k}\tilde{\xi}\right)}{\tau_f + \tau_l + \tau_p} + \frac{1}{2(\tau_f + \tau_l + \tau_p)}\right). \tag{51}$$

Taking logs on both sides, we obtain

$$\ln I = \ln\left(\frac{\beta}{c}\right) + \left(\frac{\tau_f\bar{f} + \tau_l s_l + \tau_p\left(\tilde{f} + \frac{k}{1+k}\sigma_c\tilde{\epsilon}_c + \frac{\sigma_s}{1+k}\tilde{\xi}\right)}{\tau_f + \tau_l + \tau_p} + \frac{1}{2(\tau_f + \tau_l + \tau_p)}\right). \tag{52}$$

We can define the nonfundamental volatility of the real investment as the volatility of

$$\frac{(\tau_f + \tau_l + \tau_p)\left(\ln I - \ln\left(\frac{\beta}{c}\right)\right) - \frac{1}{2} - \tau_f\bar{f}}{\tau_l + \tau_p} - \tilde{f}$$

$$= \frac{\tau_l\sigma_l\epsilon_l + \tau_p\left(\frac{k}{1+k}\sigma_c\tilde{\epsilon}_c + \frac{\sigma_s}{1+k}\tilde{\xi}\right)}{\tau_l + \tau_p} \tag{53}$$

It is straightforward to show that when $k = k_{OP} = \tau_c/(\tau_s\tau_\xi)$, $\tau_p = \tau_c + \tau_s\tau_\xi$, and the nonfundamental volatility of the real investment is the lowest, which is

$$\text{Nonfundamental volatility(real investment)} = \frac{1}{\tau_l + \tau_c + \tau_s\tau_\xi}. \quad \square \tag{54}$$

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