

# Financial Market Structure and Risk Concentration

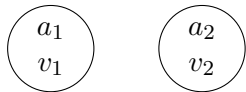
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Discussion: Chaojun Wang  
The Wharton School, University of Pennsylvania

Board of Federal Reserve  
March, 2024

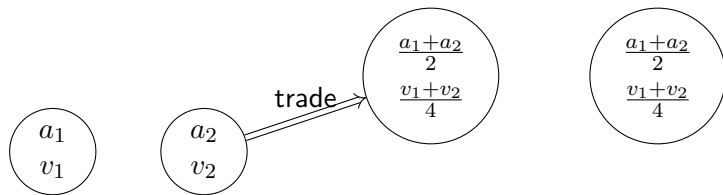
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2 agents:



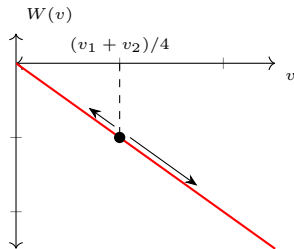
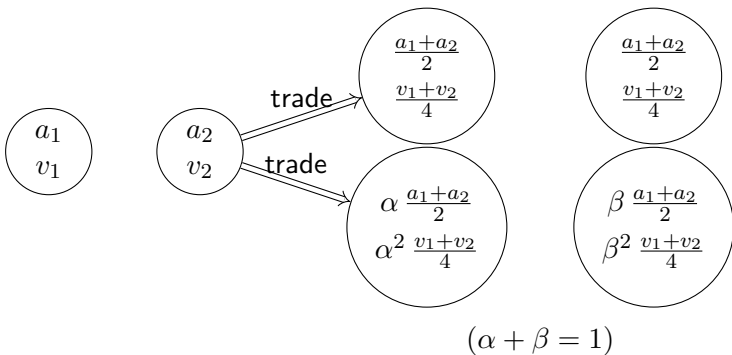
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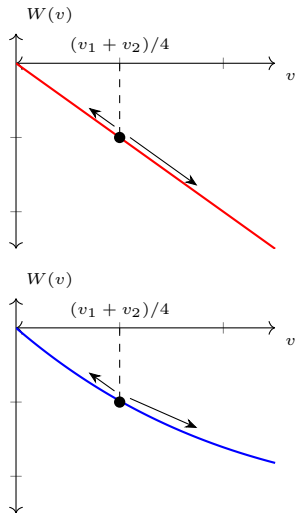
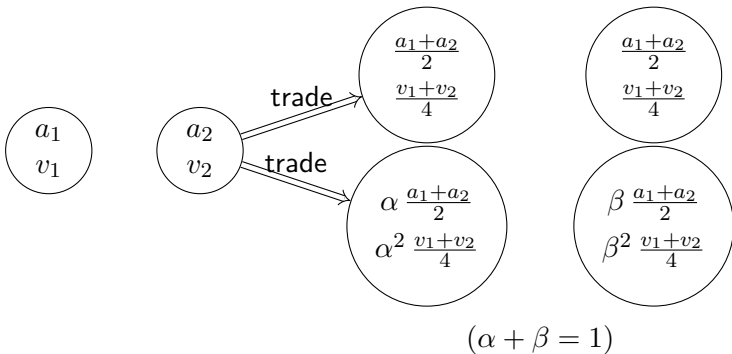
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## Suggestion #1: Sharpen the main result

- When  $W$  is linear/concave, outcome = risk sharing + random matching
- When  $W$  is only slightly convex, outcome = risk sharing + random matching
- When  $W$  is only sufficiently convex, outcome = risk concentration + PAM

## Suggestion #1: $\widetilde{W}(\sigma) = W(v)$

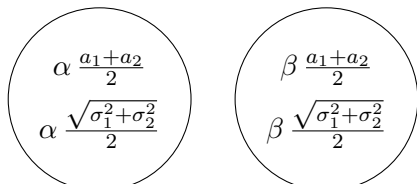
Reparametrize:

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Two circles are shown side-by-side. The left circle contains the formulas  $\alpha \frac{a_1+a_2}{2}$  and  $\alpha \frac{\sqrt{\sigma_1^2+\sigma_2^2}}{2}$ . The right circle contains the formulas  $\beta \frac{a_1+a_2}{2}$  and  $\beta \frac{\sqrt{\sigma_1^2+\sigma_2^2}}{2}$ . Below the circles is the equation  $(\alpha + \beta = 1)$ .

$$\left( \begin{array}{l} \alpha \frac{a_1+a_2}{2} \\ \alpha \frac{\sqrt{\sigma_1^2+\sigma_2^2}}{2} \end{array} \right) \quad \left( \begin{array}{l} \beta \frac{a_1+a_2}{2} \\ \beta \frac{\sqrt{\sigma_1^2+\sigma_2^2}}{2} \end{array} \right)$$

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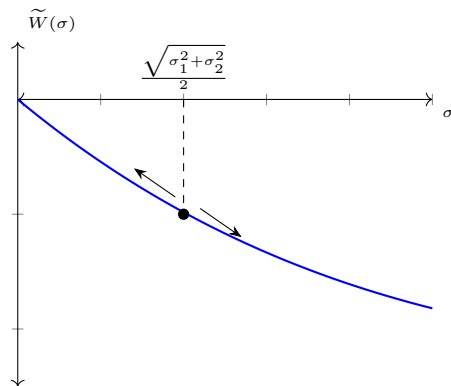
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- Extending this paper: If investors can get rid of systematic risk at a fixed cost, then more efficient to concentrate systematic risk among a small subset of investors
- How can one get rid of “systematic” risk?
- Define “systematic” risk as aggregate risk *within* the OTC segment
- Can get rid of the “OTC” risk in the larger market



## Suggestion #3: Dealers hold more assets?

- Risk = Risk of holding asset(s)
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- Systematic risk = holding of the risky market portfolio

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- Trade off between risk sharing and risk concentration
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- Main result: If investors can get rid of risk at a constant cost, more efficient to concentrate the risk among few investors
- Main suggestions:
  - 1 Sharpen the main result ( $\widetilde{W}(\sigma) = W(v)$ )
  - 2 Better interpretation of risk sharing (diversification across multiple multiple assets)
  - 3 Interpretation of risk (level of asset holding? dispersion of asset holding?)